

HS - 4

(41)

$$I_{HS} = A_D A T^2 \exp\left(-\frac{q\Phi_B}{k_B T}\right);$$

$$I_{SH} \propto n(\phi); \quad n(\phi) = N_C \exp\left(\frac{E_F - E_C(\phi)}{k_B T}\right) = N_C \exp\left(-\frac{q\Phi_B}{k_B T}\right);$$

$$n(\infty) = N_C \exp\left(\frac{E_F - E_C(\infty)}{k_B T}\right) \rightarrow N_C = N_D \exp\left(\frac{E_C(\infty) - E_F}{k_B T}\right)$$

$$\rightarrow n(\phi) = N_D \exp\left(\frac{E_C(\infty) - E_F - q\Phi_B}{k_B T}\right) = N_D \exp\left(-\frac{qV_{bi}}{k_B T}\right) = N_D \exp\left(-\frac{V_{bi}}{V_T}\right);$$

$$\rightarrow n(\phi) \propto N_D \exp\left(-\frac{V_{bi} - V_d}{V_T}\right); \quad n'(\phi) = n(\phi) - \dots = 0$$

$$= N_D \exp\left(-\frac{V_{bi}}{V_T}\right) \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right]$$

Alternative: usare modello drift-diff:

$$J_n = q n \mu_n \mathcal{E} + q D_n \frac{dn}{dx};$$

$$\text{Considero } \mathcal{E} \text{ come: } \mathcal{E} = -\frac{\partial E_C}{\partial x}$$

$$\rightarrow J_n = +q \left[n \mu_n \frac{\partial E_C}{\partial x} + D_n \frac{dn}{dx} \right] = q D_n \left[\frac{n}{N_C} \frac{\partial E_C}{\partial x} + \frac{dn}{dx} \right];$$

$$\rightarrow \int_0^{w_D} J_n \exp\left(\frac{E_C(x)}{k_B T}\right) dx = q D_n \left[n(x) \exp\left(\frac{E_C(x)}{k_B T}\right) \right] \Big|_0^{w_D}$$

$$\text{dove: } E_C(0) = q\Phi_B; \quad E_C(\infty) = q(\Phi_n + V_d);$$

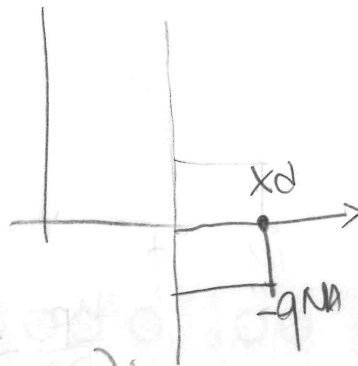
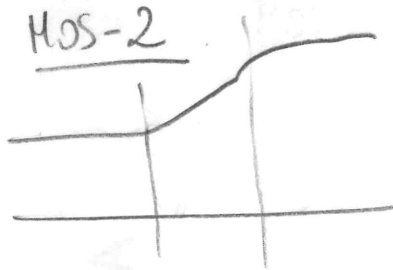
$$n(0) = N_C \exp\left(-\frac{q\Phi_B}{k_B T}\right); \quad n(\infty) = N_C \exp\left(-\frac{q\Phi_n}{k_B T}\right);$$

sostituendo e tranne;

$$J_n = \frac{q N_C D_n \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right]}{\int_0^{w_D} \exp\left(\frac{E_C(x)}{k_B T}\right) dx}$$

$$E_C(x) = q\Phi_B - \frac{q^2 N_D}{\epsilon_s} \left[x w_D - \frac{x^2}{2} \right]$$

MOS-2



$$\phi(x) = -\frac{qN_A}{\epsilon_s} [x - x_d] = \frac{qN_A}{\epsilon_s} [x_d - x]$$

$$\phi(x) = \frac{qN_A}{2\epsilon_s} [x - x_d]^2; \quad \phi(\phi) = \frac{qN_A}{2\epsilon_s} x_d^2$$

$$\phi(\phi) = +\frac{qN_A}{\epsilon_{ox}} x_d; \quad \phi(t_{ox}) = \frac{qN_A}{\epsilon_{ox}} x_d t_{ox}$$

$$\Phi_{bi} = \frac{qN_A}{2\epsilon_s} x_d^2 + \frac{qN_A}{\epsilon_{ox}} t_{ox} x_d \rightarrow x_d^2 + \frac{2\epsilon_s}{\epsilon_{ox}} t_{ox} x_d - \frac{2\epsilon_s}{qN_A} \Phi_{bi} = \phi$$

$$\rightarrow -\frac{\epsilon_s}{\epsilon_{ox}} \pm \sqrt{\left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox}\right)^2 + \frac{2\epsilon_s}{qN_A} \Phi_{bi}}$$

JFET-1

$$Q_n = -qN_D \left[\frac{a - x_d}{2} \right], \quad x_d = [\text{Schottky}] = \sqrt{\frac{2\epsilon_s}{qN_D} (\Phi_{bi} - V_d)}$$

$$= -qN_D a \left[1 - \frac{x_d}{2} \right] = -qN_D a \left[1 - \sqrt{\frac{2\epsilon_s (\Phi_{bi} - V_d)}{qN_D a^2}} \right]$$

$$Q_n = \phi \Rightarrow V_{bi} + V_{gs} - V_{gs} = \frac{qN_D}{2\epsilon_s} a^2 \rightarrow V_{gs}|_{\text{ord}} = \frac{qN_D}{2\epsilon_s} a^2 - V_{bi}$$

$$\rightarrow V_{th} = V_{bi} - \frac{qN_D}{2\epsilon_s} a^2; \quad -(V_{th} - V_{bi}) = \frac{qN_D}{2\epsilon_s} a^2$$

$$\rightarrow -qN_D a \left[1 - \sqrt{\frac{V_{bi} - (V_{gs} - \phi_{ch})}{V_{bi} - V_{th}}} \right] = -qN_D a \left[1 - \sqrt{1 - \frac{V_{gs} - (\phi_{ch} + V_{th})}{V_{bi} - V_{th}}} \right]$$

So che:

$$\frac{d^2 \phi}{dx^2} = -\frac{\rho(x)}{\epsilon_s} \Rightarrow \rho(x) = q \left[p(x) - n_p(x) - N_A + N_D \right];$$

So che: $p(x) = n_i \exp\left(\frac{E_{Fi}(x) - E_F}{k_B T}\right); \quad n_p(x) = n_i \exp\left(\frac{E_F - E_{Fi}(x)}{k_B T}\right);$

definisco $q\phi(x) = E_F - E_{Fi}(x) \Rightarrow p(x) = n_i \exp\left(-\frac{q\phi(x)}{V_T}\right);$

$$n(x) = n_i \exp\left(\frac{q\phi(x)}{V_T}\right);$$

Per $x \rightarrow \infty, \quad p_p(x) = N_A = n_i \exp\left(\frac{E_F - E_{Fi}(\infty)}{k_B T}\right) = n_i \exp\left(\frac{q\phi_p}{k_B T}\right);$

$$n_p(x) = \frac{n_i^2}{N_A} = n_i \exp\left(-\frac{q\phi_p}{k_B T}\right);$$

$$n_i = n_{p0} \exp\left(+\frac{q\phi_p}{k_B T}\right); \quad n_i = p_{p0} \exp\left(-\frac{q\phi_p}{k_B T}\right);$$

$$\hookrightarrow p_p(x) = p_{p0} \exp\left(-q \frac{\phi(x) - \phi_p}{k_B T}\right); \quad n_p(x) = n_{p0} \exp\left(-q \frac{\phi_p - \phi(x)}{k_B T}\right);$$

definisco: $\psi(x) \triangleq \frac{q(\phi(x) - \phi_p)}{V_T}$

$$\rightarrow p_p(x) = p_{p0} \exp\left(\frac{\psi(x)}{V_T}\right); \quad n_p(x) = n_{p0} \exp\left(\frac{\psi(x)}{V_T}\right);$$

Ma: @ ∞ ho neutralità:

$$p_{p0} - n_{p0} - N_A = 0 \Rightarrow N_A = p_{p0} - n_{p0}$$

$$\hookrightarrow \frac{d^2 \phi}{dx^2} = \frac{q}{\epsilon_s} \left[p_{p0} \left[\exp\left(\frac{\psi(x)}{V_T}\right) - 1 \right] - n_{p0} \left[\exp\left(-\frac{\psi(x)}{V_T}\right) - 1 \right] \right]$$

05/02/04 - compito A

2) Usando il formulario, vedo che:

$$\beta_F = 150 = \frac{\alpha_F}{1 - \alpha_F} \rightarrow \left(\frac{1}{\alpha_F} - 1 \right) \times 150 = 1 \rightarrow \alpha_F = \left(\frac{1}{151} + 1 \right)^{-1} = \frac{150}{151} = 99.34\%$$

$$\alpha_F = \beta_F = \left(1 - \frac{W_B^2}{2L_{NB}^2} \right) \left(1 + \frac{N_B W_B D_{PE}}{N_E W_E D_{NB}} \right)^{-1}$$

Dove, calcoli mi danno:

$$\left\{ \begin{array}{l} D_{PE} = 5.2; \\ D_{NB} = 20.8; \\ L_{NB} = 1.442 \cdot 10^{-3}. \end{array} \right\} \text{ tutto in cm}$$

Questa è un'equazione; per la seconda

ricordo che:

$$A_E = 1 \mu m^2 = 10^{-4} \mu m^2 \text{ cm} \quad (\mu m \text{ lo schiavo}) = 10^{-2} \text{ cm}^2$$

Ricordo che, infine, la legge di Ohm afferma:

$$R_E = \rho_E \frac{W_E}{A_E} = \frac{L}{N_E \mu_{NE} q} \cdot \frac{W_E}{A_E} \leq 1 \Omega \Rightarrow \boxed{\frac{W_E}{N_E} \leq q \mu_{NE} A_E}$$

$$\rightarrow \alpha_F = \left(1 - \frac{W_B^2}{2L_{NB}^2} \right) \left(1 + \frac{N_B W_B D_{PE}}{q \mu_{NE} A_E N_E^2 D_{NB}} \right)^{-1} = \frac{150}{151}$$

Terza "implantata" condizione: essendo un BJT, $N_E \gg N_B$. Come parametro libero scelgo proprio $N_E = 5 \cdot 10^{17}$ (10 volte N_B), e da qui posso calcolare, mediante calcolatrice, W_B :

$$W_B = 1.6 \mu m;$$

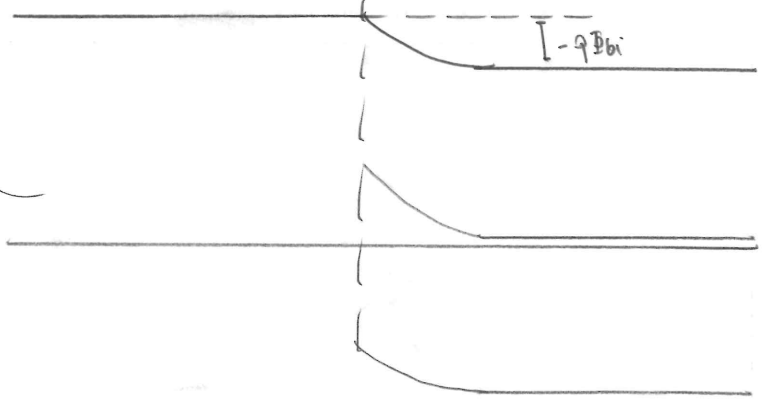
$$W_E = 0.560 \text{ cm} \rightarrow 5.6 \text{ mm} \quad (\text{mi sembra tanto}).$$

5/2/04 - compito B

(72)

2) Non chiedendo nulla, fingo che sul formulario non ci sia e parto da:

$$x_d = \sqrt{\frac{2\epsilon_s}{qN_D} (V_{bi} - V)}$$



$$V_{bi} = q\Phi_M - q\Phi_{sn} =$$

$$= q\Phi_M - \left(q\chi_s + \frac{E_g}{2} - (E_F - E_{ri}) \right) =$$

$$= q\Phi_M - \left(q\chi_s + \frac{E_g}{2} - k_B T \ln \left(\frac{N_D}{n_i} \right) \right) =$$

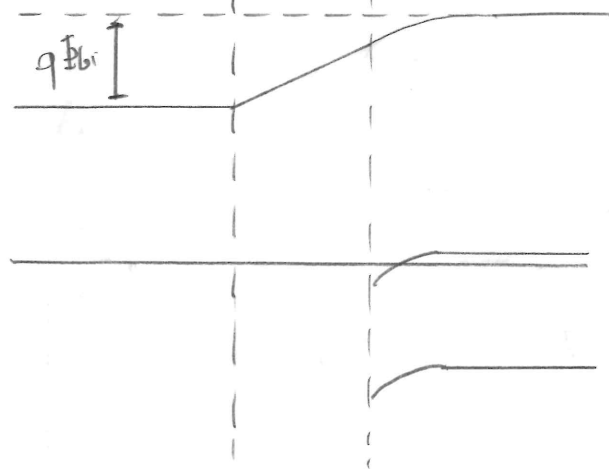
$$= q\Phi_M - q\chi_s - \frac{E_g}{2} + k_B T \ln \left(\frac{N_D}{n_i} \right) = 1.051 \text{ eV}$$

$$Q_d = +qN_D x_d = \sqrt{2qN_D \epsilon_s (V_{bi} - V)}$$

$$C_d = A \left| \frac{dQ_d}{dV} \right| = \frac{L + 2qN_D \epsilon_s}{2 \sqrt{2qN_D \epsilon_s (V_{bi} - V)}} = \frac{1}{2} \sqrt{\frac{2qN_D \epsilon_s}{V_{bi} - V}} = \sqrt{\frac{qN_D \epsilon_s}{2(V_{bi} - V)}}$$

$$V_{bi} = 1.051 \text{ V}$$

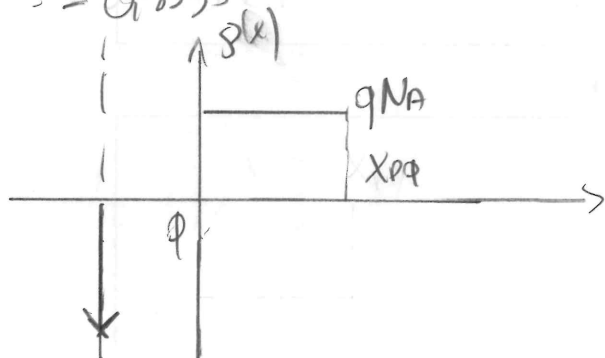
$$C_d = 2.663 \text{ pF} = 2.663 \times 10^{-12} \text{ F}$$



$$q\Phi_{bi} = q\Phi_M - q\Phi_{Sn} = q\Phi_M - \left(q\chi_s + \frac{E_g}{2} + (E_{Fi} - E_F) \right)$$

$$= q\Phi_M - q\chi_s - \frac{E_g}{2} - k_B T \ln\left(\frac{N_A}{n_i}\right) =$$

$$= -0.8595$$



$$E(x) = \int \frac{\rho(x)}{\epsilon_s} dx = \frac{qN_A}{\epsilon_s} x + C ;$$

$$\frac{qN_A}{\epsilon_s} x_{\phi\phi} + C = \phi$$

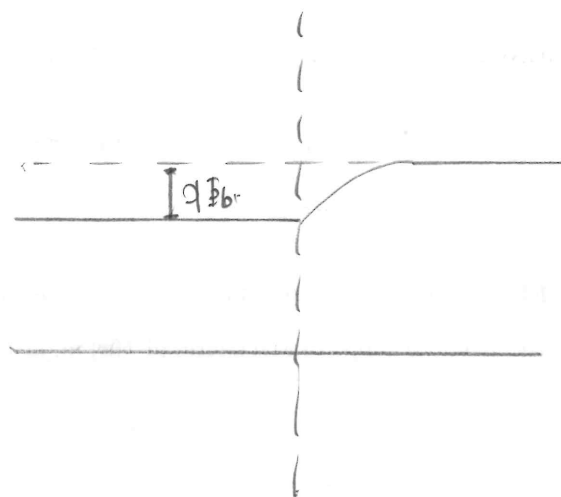
$$\rightarrow E(x) = \frac{qN_A}{\epsilon_s} [x - x_{\phi\phi}] ; (x \geq \phi) \rightarrow E(x) = \frac{qN_A}{\epsilon_s} [x - x_{\phi\phi}] (x \geq \phi) ;$$

$$\phi(x) = - \int E(x) dx = - \frac{qN_A}{2\epsilon_s} [x - x_{\phi\phi}]^2 + C ;$$

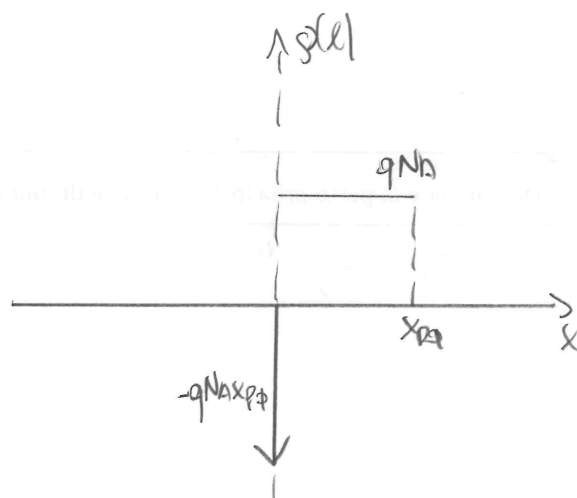
$$@ x = x_{\phi\phi}, \phi(x) = \phi \Rightarrow C = \phi !$$

$$\text{for } L \times L \phi, E(x) = \text{costante} ;$$

$$E(\phi^-) = E(\phi^+) \frac{\epsilon_s}{\epsilon_{ox}} = - \frac{qN_A}{\epsilon_{ox}} x_{\phi\phi} ;$$



$$q\Phi_{bi} = -0.8595 \text{ eV.}$$



$$E(x) = \frac{qN_A}{\epsilon_s} [x - x_{\phi\phi}] (x \geq \phi) ;$$

$$\phi(x) = - \frac{qN_A}{2\epsilon_s} [x - x_{\phi\phi}]^2 ;$$

$$\rightarrow \Phi_i = \phi(\phi) = - \frac{qN_A}{2\epsilon_s} x_{\phi\phi}^2 ;$$

$$Q(x) = \int \frac{Q_{Na}}{\epsilon_{ox}} x_{pp} = \frac{Q_{Na}}{\epsilon_{ox}} x_{pp} x + C;$$

(ignoro "C" e faccio in modo da avere:

$$Q(+t_{ox}) = \frac{Q_{Na}}{\epsilon_{ox}} x_{pp} t_{ox};$$

$$\Phi_{bi} = \frac{Q_{Na}}{\epsilon_{ox}} x_{pp} t_{ox} - \frac{q N_A}{2 \epsilon_s} x_{pp}^2$$

$$\hookrightarrow x_{pp}^2 - 2 \frac{\epsilon_s}{\epsilon_{ox}} t_{ox} x_{pp} - \frac{2 \epsilon_s}{q N_A} \Phi_{bi} = 0$$

$$\hookrightarrow \frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \pm \sqrt{\left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \right)^2 + \frac{2 \epsilon_s}{q N_A} \Phi_{bi}}$$

$$Q = q N_A x_p = \frac{1}{2} \frac{\frac{2 \epsilon_s}{q N_A} \left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \right)^2 + \frac{2 \epsilon_s}{q N_A} \Phi_{bi}}{\sqrt{\left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \right)^2 + \frac{2 \epsilon_s}{q N_A} \Phi_{bi}}}$$

$$= 11.78 \mu F/cm^2;$$

$$C_{ox} = \frac{\epsilon_{ox}}{t_{ox}} = 67.29 \text{ nF/cm}^2$$



$$\hookrightarrow C = 66.91 \text{ nF/cm}^2 !$$

$$\hookrightarrow x_{pp} = \pm \sqrt{\frac{2 \epsilon_s}{q N_A} \Phi_{bi}} \quad (24)$$

$$\hookrightarrow q N_A x_{pp} = \sqrt{2 q N_A \epsilon_s (\Phi_{bi} - V_0)};$$

$$\frac{dQ}{dV_0} = \frac{1}{2} \frac{-q^2 N_A \epsilon_s}{\sqrt{2 q N_A \epsilon_s (\Phi_{bi} - V_0)}}$$

$$= \sqrt{\frac{q N_A \epsilon_s}{2 (\Phi_{bi} - V_0)}}$$

$$\hookrightarrow C_{HS} = 19.59 \text{ nF/cm}^2 !$$

Valutare tensione di soglia della struttura MOS.

Si ha, dal formulone:

$$V_{th} = V_{th\phi} + \cancel{V_{FB}} \dots$$

dove:

$$V_{th\phi} = V_{FB} + 2 \phi_p + \cancel{V_{FB}} \dots$$

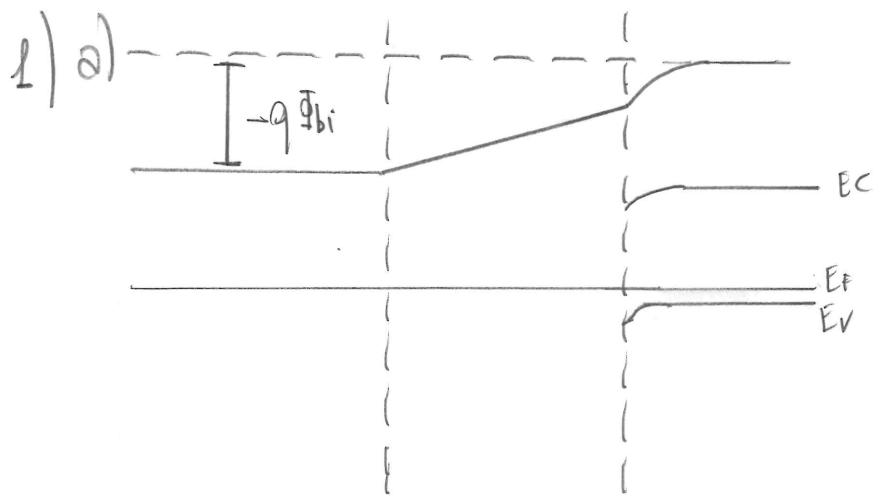
e

$$q \phi_p = E_{Fi} - E_F = q V_T \ln \frac{N_A}{n_i} = 0.3495 \text{ eV}$$

$$V_{th\phi} = V_{th} = 2 \phi_p + V_{FB} = \underline{1.559 \text{ V}}$$

Esercizi di prova

(75)



$$\begin{aligned}
 q\Phi_{bi} &= q\Phi_N - q\Phi_S = \\
 &= q\chi_s - \left(q\chi_s + \frac{E_g}{2} + |E_F - E_F| \right) \\
 &= -k_B T \ln \left(\frac{N_A}{n_i} \right) - \frac{E_g}{2} = \\
 &= \boxed{-0.91 \text{ eV}}
 \end{aligned}$$

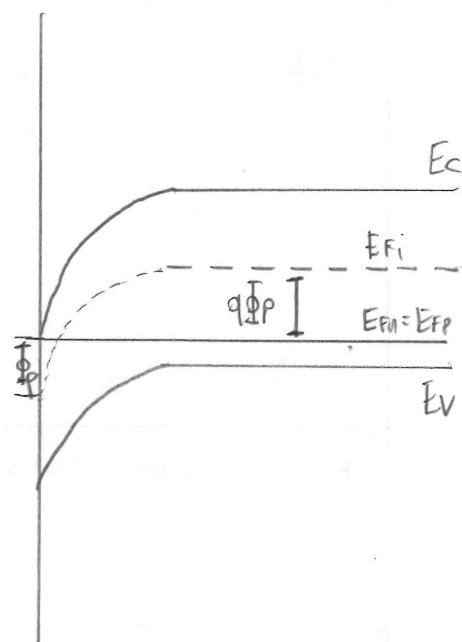
$$\hookrightarrow V_{FB} = -0.91 \text{ V}$$

Dal formulario, ricordando che V_{FB} è la tensione applicata dall'esterno che porta il livello del vuoto a esser costante. Il "+" sta sul metallo SEMPRE.

$$-q\phi_p = 0.3495 \text{ eV}$$

$$b) \rightarrow V_{th} = V_{th0} \text{ (no body)} = 1.609 \text{ V}$$

c) Il quesito chiede sostanzialmente un diagramma a bande in forte inversione. In questo stato, i livelli sono molto incurvati:



$E_F(\phi) - E_F(\infty) = -2\phi_p$, e rimane circa bloccato a ciò.

$$d) Q_n = -C_{ox} (V_{GS} - \cancel{\phi_{th}} - V_{th}) = \boxed{-\frac{\epsilon_{ox}}{t_{ox}} (V_{GS} - V_{th})} = -93.6 \text{ nC (inversione)}$$

$$Q_d = +qN_A x_d(3V) =$$

$$e) Q_n = -C_{ox} (V_{GS} - \phi_{ch}(y) - V_{th}) \quad \phi_{ch}(y) = \text{retta che cresce da } \phi \text{ a } 2\psi$$

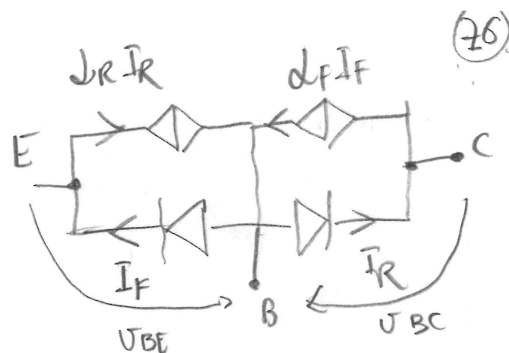
su L.

$$\frac{y-0}{0.5-0} = \frac{x-\phi}{L-\phi} \Rightarrow \boxed{y = \frac{x}{L} \cdot 0.5} \Rightarrow \boxed{\phi_{ch}(y) = \frac{y}{L} \cdot 0.5} \quad \left[\begin{array}{l} y = \phi \text{ al} \\ \text{il source.} \end{array} \right]$$

Esercizio 2

Considero il modello del transistor (iniezione):

$$\begin{cases} I_E = \alpha_R I_R - I_F \\ I_C = \alpha_F I_F - I_R \end{cases} \quad \begin{cases} I_F = I_{ES} \left[\exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right] \\ I_R = I_{CS} \left[\exp\left(\frac{V_{BC}}{V_T}\right) - 1 \right] \end{cases}$$



Valutare: α_R , α_F , I_{CS} e I_{ES} . Si sa che: $I_C = 3 \text{ nA}$, E aperto;

30 nA , E in cc con base
 450 nA , base aperto.

$V_{BC} < 0$.

1) Ricordo che: $\alpha_F I_{ES} = \alpha_R I_{CS}$.

Se l'emettitore è aperto

$$I_E = \alpha_R I_R - I_F = 0 \rightarrow \text{dato che } V_{BC} < 0, I_R \approx -I_{CS}$$

$$\rightarrow I_F = -\alpha_R I_{CS} \rightarrow I_C = \alpha_F I_F - I_R = -\alpha_F \alpha_R I_{CS} + I_{CS} = I_{CS} (1 - \alpha_F \alpha_R)$$

2) $I_E = \alpha_R I_R - I_F$, ma $I_F = 0$ ($V_{BE} = 0$)

$$\rightarrow I_C = -I_R = I_{CS}$$

$$3) I_B = -I_C - I_E = I_F + I_R - \alpha_R I_R - \alpha_F I_F = I_F (1 - \alpha_F) + I_R (1 - \alpha_R) = 0$$

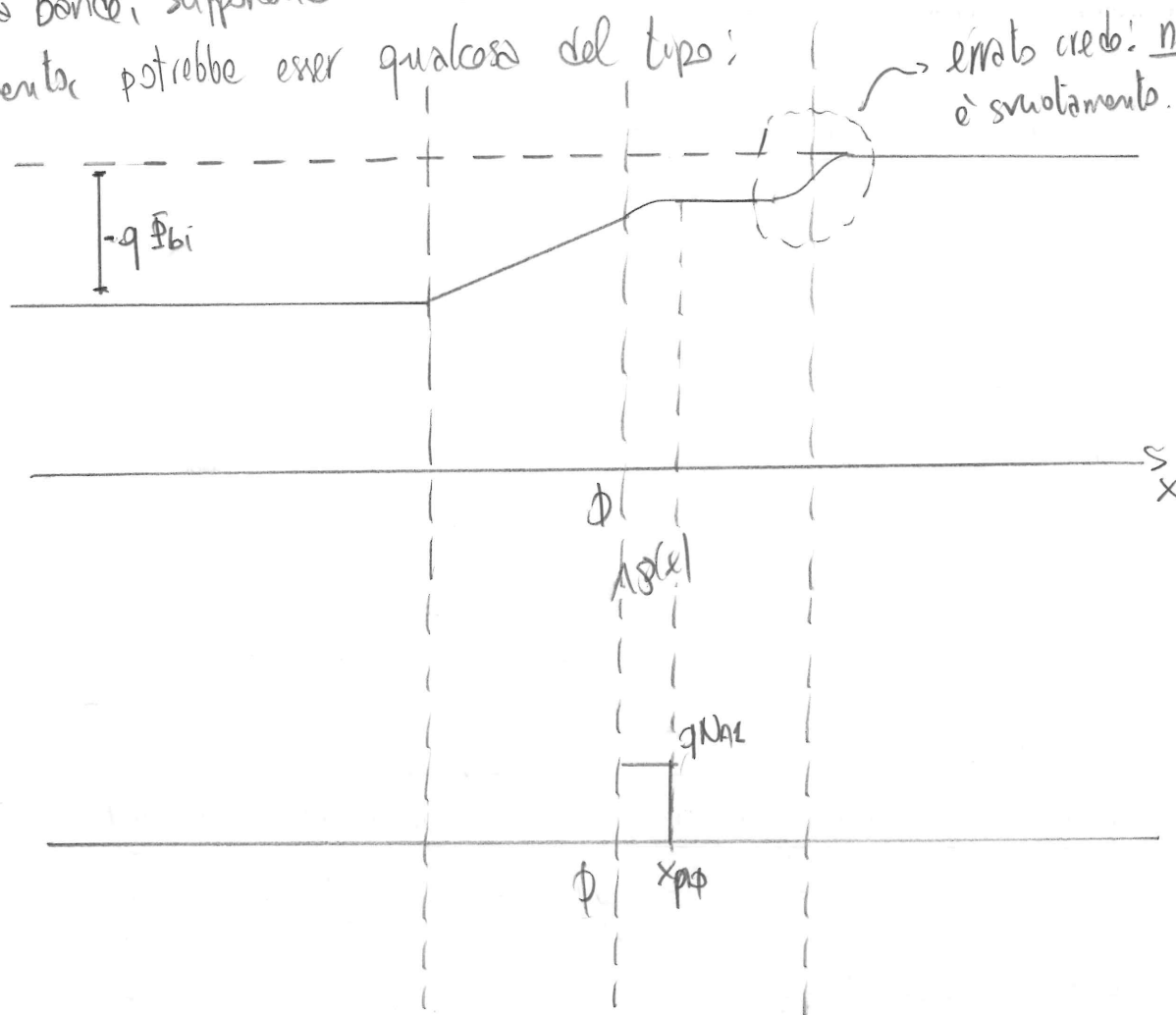
$$I_F = -I_R \frac{1 - \alpha_R}{1 - \alpha_F} = I_{CS} \frac{1 - \alpha_R}{1 - \alpha_F}$$

Risolvendo il sistema si trovano i parametri.

02/02/06 - 2

(27)

Il d. a bande, supponendo che non visia overlap delle regioni di smotamento potrebbe esser qualcosa del tipo:



$$\phi(x) = \int \frac{qN_{ac}}{\epsilon_s} dx = \frac{qN_{ac}}{\epsilon_s} [x - x_{pp}] ; \quad \psi(x) = -\frac{qN_{ac}}{2\epsilon_s} [x - x_{pp}]^2 ; \quad x > 0$$

Vorrei vedere quanto si estende x_{pp} e verificare l'ipotesi.

$$\rightarrow \psi(\phi) = -\frac{qN_{ac}}{2\epsilon_s} x_{pp}^2 ;$$

$$\phi(x) = -\frac{qN_{ac}}{\epsilon_{ox}} x_{pp} \quad (\text{nell'ossido}) ;$$

$$\rightarrow \psi(x) = \frac{qN_{ac}}{\epsilon_{ox}} x_{pp} x \Rightarrow \psi(t_{ox}) = \frac{qN_{ac}}{\epsilon_{ox}} x_{pp} t_{ox} ;$$

$$\rightarrow \psi(t_{ox}) = -\frac{qN_{ac}}{2\epsilon_s} x_{pp}^2 + \frac{qN_{ac}}{\epsilon_{ox}} x_{pp} t_{ox} = \Phi_t \quad (\Phi_t \text{ è una "barriera che non tiene conto di } N_{a2})$$

$$\rightarrow x_{pp}^2 - \frac{2\epsilon_s}{\epsilon_{ox}} t_{ox} x_{pp} + \Phi_t \frac{2\epsilon_s}{qN_{ac}} = 0 \rightarrow x_{pp} = \frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \pm \sqrt{\left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox}\right)^2 - \frac{2\epsilon_s}{qN_{ac}} \Phi_t}$$

→ Calcolo Φ_t :

$$q(\Phi_H - \Phi_S) = q\chi_s - \left[q\chi_s + \frac{E_g}{2} + |E_{Fi} - E_F| \right] = -\frac{E_g}{2} - k_B T \ln\left(\frac{N_A}{n_i}\right) = -0.9 \text{ eV}$$

↳ $X_{pp} \geq 70 \text{ nm}$.

Cosa vuol dire? Che la regione di svuotamento attraversa tutta la regione svuotata.

$$V_S = \frac{qN_{A1}}{2\epsilon_s} x_L^2 + \frac{qN_{A2}}{2\epsilon_s} (x_d^2 - x_L^2) \Rightarrow x_d = \sqrt{\frac{2\epsilon_s}{qN_{A2}} \left[V_S - \frac{q}{2\epsilon_s} (N_{A1} - N_{A2}) x_L^2 \right]}$$

@ scegli $V_S = 2\Phi_p - \cancel{V_{BS}}$ (ignoro effect body), Φ_p definito rispetto a N_{A2}

(quella dove finisce la regione di svuotamento).

$$\hookrightarrow x_d = \sqrt{\frac{2\epsilon_s}{qN_{A2}} \left[2\Phi_p - \frac{q}{2\epsilon_s} (N_{A1} - N_{A2}) x_L^2 \right]}$$

$$Q_t = -Q_n - Q_d = -C_{ox} (V_{GS} - \phi_{ch} - 2\phi_p) - qN$$

Finire

23/01/2008

2) a)

$$\Delta E_g = E_{g2} - E_{g1} = -0.225 \text{ eV};$$

$$q\Delta\chi = q\chi_2 - q\chi_1 = 0.265 \text{ eV};$$

$$q\Phi_{bi} = q\Phi_{s2} - q\Phi_{s1} = q\chi_2 + (E_c - E_f) -$$

$$+ [q\chi_1 + E_{g1} - (E_f - E_v)]$$

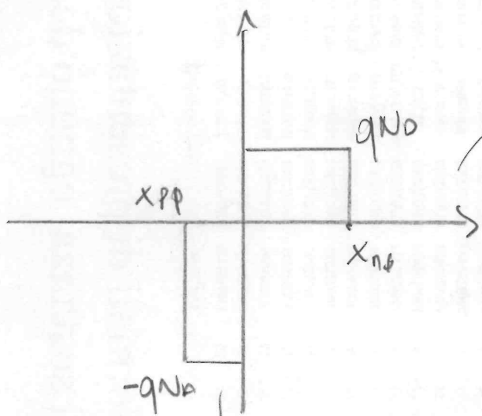
$$= q\Delta\chi - E_{g1} + k_B T \ln\left(\frac{N_{c2} N_{v1}}{N_{d2} N_{a1}}\right) = -1.32 \text{ eV}$$

Cerchiamo di capire come fa il diag. a bande: $\Delta\chi > \phi$, dunque $E_c(\phi^+) \sim E_c(\phi^-)$:

$$\Delta E_c = E_{c2} - E_{c1} = -q\Delta\chi; \quad \Delta E_c < \phi \Rightarrow \text{disc. di questo tipo.}$$

$$\Delta E_v = -q\Delta\chi - \Delta E_g = -0.04 \text{ eV}.$$

b)



$$\phi(x) = \int \frac{qND}{\epsilon_2} dx = \frac{qND}{\epsilon_2} [x - x_{n\phi}];$$

$$\phi(x) = -\frac{qND}{2\epsilon_2} [x - x_{n\phi}]^2$$

$$\hookrightarrow \phi(\phi) = -\frac{qND}{2\epsilon_2} x_{n\phi}^2;$$

$$\phi(x) = \int \frac{-qNA}{\epsilon_1} dx = -\frac{qNA}{\epsilon_1} x + C; \quad -\frac{qNA}{\epsilon_1} x_{PP} = 0$$

$$\rightarrow \phi(x) = \frac{qNA}{\epsilon_1} [x_{PP} - x]$$

$$\text{Nota: } \phi(\phi^+) = \phi(\phi^-):$$

$$\rightarrow -\frac{qND}{\epsilon_2} x_{n\phi} = \frac{qNA}{\epsilon_1} x_{PP} \quad [x_{PP} < x_{n\phi}]$$

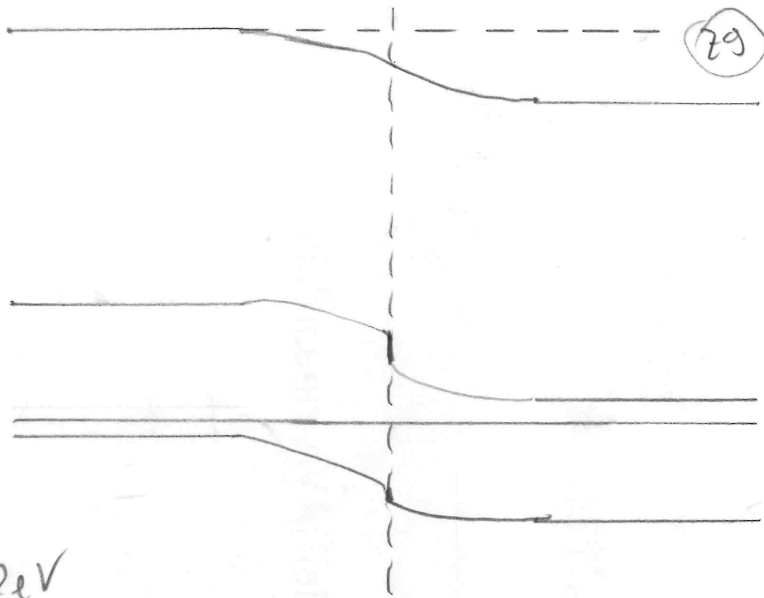
$$\phi(x) = \frac{qNA}{2\epsilon_1} [x - x_{PP}]^2$$

$$\text{Poi: } qND x_{n\phi} = qNA x_{PP} \quad ! \quad x_{PP} = \frac{ND}{NA} x_{n\phi}$$

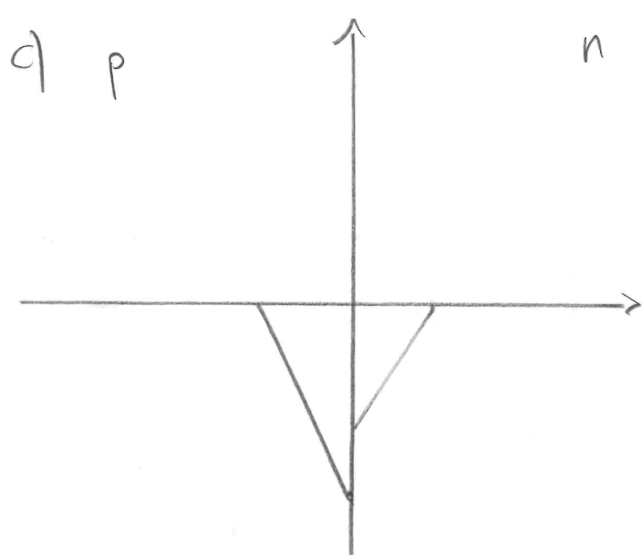
$$\Phi_{bi} = \frac{qNA}{2\epsilon_1} x_{PP}^2 + \frac{qND}{2\epsilon_2} x_{n\phi}^2 = \frac{qNA}{2\epsilon_1} \frac{ND^2}{NA^2} x_{n\phi}^2 + \frac{qND}{2\epsilon_2} x_{n\phi}^2 = \frac{qND}{2} \left[\frac{ND}{\epsilon_1 NA} + \frac{1}{\epsilon_2} \right] x_{n\phi}^2$$

$$\rightarrow = \frac{qND}{2} \left[\frac{\epsilon_2 ND + \epsilon_1 NA}{\epsilon_1 NA \epsilon_2} \right] x_{n\phi}^2 \rightarrow x_{n\phi} = \sqrt{\frac{2 \epsilon_1 NA \epsilon_2}{qND \epsilon_2 ND + \epsilon_1 NA}} \Phi_{bi}$$

$$= \sqrt{\frac{2 \epsilon_1 NA \epsilon_2 ND}{qND \epsilon_2 ND + \epsilon_1 NA}} \Phi_{bi}$$



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$$\mathcal{D}(\Phi) = \mathcal{D}(\Phi')$$

(210)

$$\hookrightarrow \epsilon_L \mathcal{E}(\Phi) = \epsilon_2 \mathcal{E}(\Phi')$$

minore è ϵ_1 , maggiore è $\mathcal{E}$.

$\hookrightarrow$ maggiore in (1).

$$\mathcal{E}(\Phi^-) = \frac{q N_A}{\epsilon_L} x_{p\Phi}.$$

d) Per far ciò, servono le leggi della giunzione. Le ricavo, per l'occasione, perché a memoria non le so.

$$p_n(x_n) n_p(x_p) = [\text{da formule}] = N_{v2} \exp\left(\frac{E_v(x_n) - E_f}{k_B T}\right) N_{c1} \exp\left(\frac{E_f - E_c(x_p)}{k_B T}\right)$$

$$\text{Per ora, @ eq. th.} \hookrightarrow = N_{c1} N_{v2} \exp\left(\frac{E_v(x_n) - E_c(x_p)}{k_B T}\right) \left\{ \begin{array}{l} E_c(x_p) - E_v(x_n) = \Delta E_c + E_{g2} \\ \Delta E_v + E_{g1} \end{array} \right.$$

Poi:

$$p_n(x_n) n_n(x_n) \approx N_{d2} p_n(x_n) = N_{v2} \exp\left(\frac{E_v(x_n) - E_f}{k_B T}\right) N_{c2} \exp\left(\frac{E_f - E_c(x_n)}{k_B T}\right) = N_{v2} N_{c2} \exp\left(-\frac{E_{g2} + q\Phi_n}{k_B T}\right)$$

$$\hookrightarrow p_n(x_n) = \frac{N_{v2} N_{c2}}{N_{d2}} \exp\left(-\frac{E_{g2}}{k_B T}\right).$$

Dunque, riscrivo l'exp come:

$$n_p(x_p) = \frac{N_{d2}}{N_{v2} N_{c2}} N_{v2} N_{c1} \exp\left(\frac{E_{g2}}{k_B T}\right) \exp\left(-\frac{\Delta E_c + \Delta E_v + E_{g2}}{k_B T}\right) = \frac{N_{c1}}{N_{c2}} N_{d2} \exp\left(-\frac{q\Phi_{bi} + \Delta E_c}{k_B T}\right).$$

Allo stesso modo si tira fuori:

$$p_n(x_n) = \frac{N_{v2}}{N_{v1}} N_{c1} \exp\left(-\frac{q\Phi_{bi} + \Delta E_v}{k_B T}\right).$$

$$\hookrightarrow n_p'(x_p) = \frac{N_{c1}}{N_{c2}} N_{d2} \exp\left(-\frac{\Delta E_c + q\Phi_{bi}}{k_B T}\right) \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right].$$

$$p_n'(x_n) = \frac{N_{v2}}{N_{v1}} N_{c1} \exp\left(-\frac{\Delta E_v + q\Phi_{bi}}{k_B T}\right) \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right];$$

e) Pongo $n_p'(x_p) = p_n'(x_n)$:

$$\frac{N_{c1}}{N_{c2}} \textcircled{N_{D2}} \exp\left(-\frac{\Delta E_c}{k_B T}\right) = \frac{N_{v2}}{N_{v1}} N_{A2} \exp\left(-\frac{\Delta E_v}{k_B T}\right).$$

$$\hookrightarrow N_{D2} = N_{A2} \frac{N_{v2} N_{c2}}{N_{v1} N_{c1}} \exp\left(-\frac{\Delta E_v - \Delta E_c}{k_B T}\right).$$

Cosa capita in una omegianzione? Consideriamo, dal formulario, le tradizionali leggi della giunzione:

$$n_p(x_p) = n_{p0}(x_p) \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right] ; \quad p_n(x_n) = p_{n0}(x_n) \left[\exp\left(\frac{V_d}{V_T}\right) - 1 \right]$$

Queste si possono ottenere considerando che $N_{v2} = N_{v1}$, $N_{c2} = N_{c1}$, $\Delta E_v = \Delta E_c = \phi$, e avendo "degenerare" le leggi della giunzione generalizzate.

$n_p(x_p) = p_n(x_n) \implies n_{p0}(x_p) = p_{n0}(x_n)$
che è quello che si ottiene degenerando le equazioni.

Faccio un po' di conto:

b) $x_{np} = 257 \text{ nm}$; $x_{pp} = x_{np} \frac{N_D}{N_A} = 1029 \text{ nm}$;

c) $E(\phi^-) = 79,06 \text{ kV/cm}$ (contro 76 e rotti in ϕ^+ !)

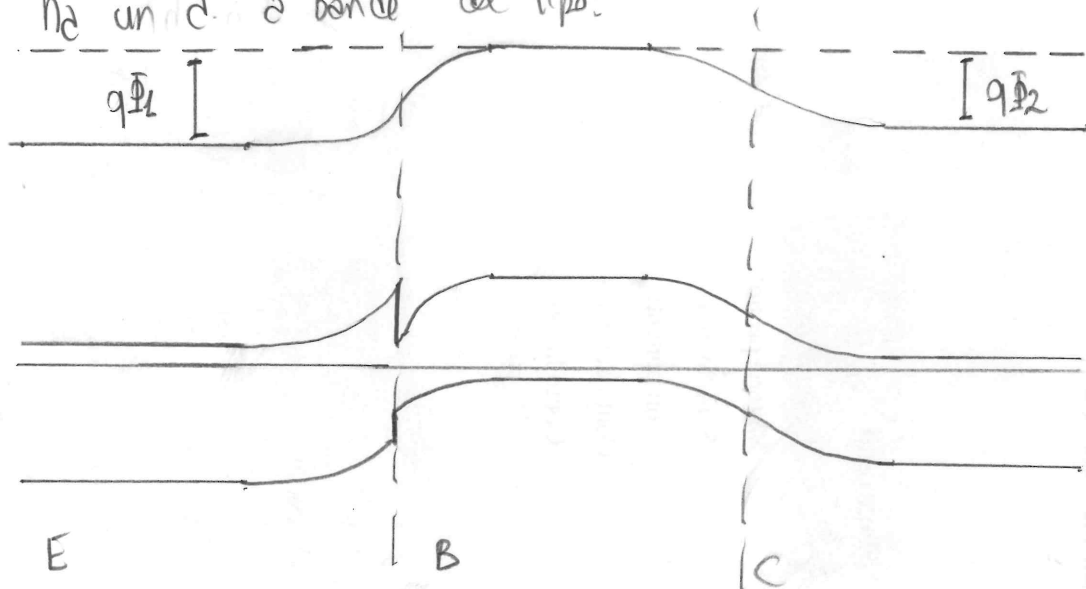
d) $n_p'(x_p) = 3,416 \text{ E } 15$;

$p_n'(x_p) = 0,44 \text{ E } 10.$

04/02/08

712

a) La struttura ha un d.o.b. del tipo:



$$\Delta E_g = 0.136 \text{ eV}$$

$$\Delta E_c = 0.291 \text{ eV}$$

$$\Delta E_v = 0.136 \text{ eV}$$

$$q\Phi_c = q\Phi_B - q\Phi_E = \left[q\chi_B + E_{gB} - (E_F - E_v) \right] - \left[q\chi_E + (E_c - E_F) \right]$$

$$= q\Delta\chi + E_{gB} + k_B T \ln \left(\frac{N_{AB} N_{DE}}{N_{VB} N_{CE}} \right) = 1.716 \text{ eV}$$

$$q\Phi_2 = q\Phi - q\Phi_B = \left[q\chi_c + (E_c - E_F) \right] - \left[q\chi_B + E_{gB} - (E_F - E_v) \right]$$

$$= -E_{gB} + k_B T \ln \left(\frac{N_{VB} N_{CC}}{N_{AB} N_{DC}} \right) = -1.323 \text{ eV}$$

b) Ricordo la definizione di γ_F :

$$\gamma_F = \frac{J_{ns}(x_{BE})}{J_{nB}(x_{BE}) + J_{pE}(x_{EB})}$$

Calcolo $p_n'(x)$: considero ipotesi lato "caro":

$$\hookrightarrow \phi = -\frac{q}{\epsilon} \frac{\partial J_p}{\partial x} - \frac{p_n'}{q_p} \rightarrow \partial_p = \frac{\partial p_n'}{\partial x} D_n \rightarrow \frac{\partial^2 p_n'(x)}{\partial^2} = \frac{p_n'(x)}{L_p^2}$$

$$\hookrightarrow p_n'(x) = A \exp\left(\frac{x}{L_p}\right) + B \exp\left(-\frac{x}{L_p}\right); \quad p_n'(x_E) = \phi = A \exp\left(\frac{x_E}{L_p}\right) + B \exp\left(-\frac{x_E}{L_p}\right)$$

$$\hookrightarrow B = -A \exp\left(\frac{2x_E}{L_p}\right);$$

$$p_n'(x_{EB}) = A \exp\left(\frac{x_{EB}}{L_p}\right) - A \exp\left(-\frac{x_{EB}}{L_p}\right) \exp\left(\frac{2x_E}{L_p}\right)$$

$$\rightarrow A \left[\exp\left(\frac{x_{EB}}{L_p}\right) - \exp\left(-\frac{x_{EB} - 2x_E}{L_p}\right) \right] = p_n'(x_{EB}) \rightarrow A = \frac{p_n'(x_{EB}) \exp\left(-\frac{x_E}{L_p}\right)}{2 \sinh\left(\frac{x_{EB} - x_E}{L_p}\right)}$$

$$B = - \frac{p_n'(x_{EB}) \exp\left(\frac{x_E}{L_p}\right)}{2 \sinh\left(\frac{x_{EB} - x_E}{L_p}\right)}$$

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$$\begin{aligned} \rightarrow p_n'(x) &= \frac{1}{2 \sinh\left(\frac{x_{EB} - x_E}{L_p}\right)} \left[p_n'(x_{EB}) \exp\left(\frac{x - x_E}{L_p}\right) - p_n'(x_E) \exp\left(\frac{x_E - x}{L_p}\right) \right] = \\ &= \frac{2 \sinh\left(\frac{x - x_E}{L_p}\right)}{2 \sinh\left(\frac{x_{EB} - x_E}{L_p}\right)} p_n'(x_{EB}) \stackrel{\text{Taylor}}{\approx} \phi \quad \boxed{\frac{x - x_E}{x_{EB} - x_E} p_n'(x_{EB})} \end{aligned}$$

$$J_p(x_{EB}) = \left. \frac{\partial p_n'(x)}{\partial x} \right|_{x_{EB}} = q D_n \frac{p_n'(x_{EB})}{x_E} =$$

Considerando $x_{BE} = \phi$, deveria avere:

$$n_p'(x) = n_p'(\phi) \frac{\sinh\left(\frac{x_B - x}{L_n}\right)}{\sinh\left(\frac{x_B}{L_n}\right)} + n_p'(x_B) \frac{\sinh\left(\frac{x}{L_n}\right)}{\sinh\left(\frac{x_B}{L_n}\right)}$$

Derivo e valuto in $x = \phi$:

$$\rightarrow \left. \frac{\partial n_p'(x)}{\partial x} \right|_{\phi} = - \frac{n_p'(\phi)}{L_n} \frac{\cosh\left(\frac{x_B - \phi}{L_n}\right)}{\sinh\left(\frac{x_B}{L_n}\right)} + \frac{n_p'(x_B)}{L_n} \frac{\cosh\left(\frac{\phi}{L_n}\right)}{\sinh\left(\frac{x_B}{L_n}\right)} =$$

$$= - \frac{n_p'(\phi)}{L_n} \coth\left(\frac{x_B}{L_n}\right) + \frac{n_p'(x_B)}{L_n} \left[\sinh\left(\frac{x_B}{L_n}\right) \right]^{-1}$$

$$\approx - \frac{n_p'(\phi)}{x_B} + \frac{n_p'(x_B)}{x_B} \rightarrow J_n(\phi) = q D_n \left. \frac{\partial n_p}{\partial x} \right|_{\phi} \stackrel{\text{approx. RAD}}{\approx} \frac{q D_n}{x_B} \left[n_p'(\phi) - n_p'(x_B) \right]$$

$$n_p'(\phi) = \frac{N_{CB}}{N_{CE}} N_{DE} \exp\left(-\frac{q \phi_i + \delta E_C}{k_B T}\right) \left[\exp\left(\frac{V_{BE}}{V_T}\right) - 1 \right];$$

$$p_n'(x_n) = \frac{N_{VE}}{N_{VB}} N_{AB} \exp\left(-\frac{q \phi_i + \delta E_V}{k_B T}\right) \left[\exp\left(\frac{V_{AB}}{V_T}\right) - 1 \right];$$

$$\rightarrow \gamma_F = \left[1 + \frac{J_{pE}(x_{EB})}{J_{pB}(x_{BE})} \right]^{-1} = \left[1 + \frac{N_{VE} N_{AB} D_E x_B N_{CE} \exp\left(-\frac{\delta E_C}{k_B T}\right)}{N_{VB} N_{CB} N_{DE} x_E D_n \exp\left(-\frac{\delta E_V}{k_B T}\right)} \right]^{-1}$$

c) A destra ho una giunzione p-n:

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$$\epsilon_s = 131 \text{ ; } X_p = x_d \frac{N_{dc}}{N_{dc} + N_{AB}} = \frac{N_{dc}}{N_{dc} + N_{AB}} \sqrt{\frac{2\epsilon_s}{q} \left[\frac{1}{N_{AB}} + \frac{1}{N_{dc}} \right] (V_{bi} - V_b)} =$$

$$= 21 \text{ nm ;}$$

Per l'altra, discorso simile, ma con cambio di ϵ !

$$\frac{q N_{DE}}{2\epsilon_E} x_{np}^2 + \frac{q N_{AB}}{2\epsilon_B} x_{pn}^2 = \Phi_L \rightarrow x_{na} = \frac{N_{AB}}{N_{DE}} x_{pd}$$

$$\hookrightarrow \frac{q N_{DE}}{2\epsilon_E} \frac{N_{AB}^2}{N_{DE}^2} x_{pd}^2 + \frac{q N_{AB}}{2\epsilon_B} x_{pd}^2 = \Phi_L$$

$$\hookrightarrow \frac{q N_{AB}}{2} \left[\frac{N_{AB}}{\epsilon_E N_{DE}} + \frac{1}{\epsilon_B} \right] x_{pd}^2 = \Phi_L$$

$$\rightarrow x_{ex} = \sqrt{\frac{2}{q N_{AB}} \frac{\epsilon_B \epsilon_E N_{DE}}{\epsilon_E N_{DE} + \epsilon_B N_{AB}} (V_{bi} - V_a)}$$

$$\rightarrow x_p = 8,3 \text{ nm ;}$$

$$\Rightarrow V_{AB}' = V_B - x_p - x_n = 370,1 \text{ mV}$$

d) Con un BT dalla geometria / drogaggi analoghi, avrei, con regioni di svuotamento: (in GaAs)

$$x_{p|_{sx}} = 5,6 \text{ nm} \rightarrow \text{l'unica cosa che cambia è la } \Phi_{bi} \text{ (che ho approssimato } \Phi_1' = \Phi_2).$$

$x_{p|_{dx}}$ medesimo

Cambia poco. Per migliorare si dovrebbero cambiare i drogaggi !!!

04/02/2010

Esercizio 2

a) $\Delta E_g = E_{g2} - E_{g1} = -0,34 \text{ eV}$;

$\Delta E_C = 0,204 \text{ eV}$;

$\Delta E_V = 0,136 \text{ eV}$.

$q\Phi_{bi} = q\Phi_2 - q\Phi_1 =$

$= [q\chi_2 + E_{g2}(E_F - E_V)] - [q\chi_1 + (E_C - E_F)] =$

$= q\Delta\chi + E_g + k_B T \ln \left(\frac{N_{D1} N_{A2}}{N_{C1} N_{V2}} \right) = 1,68 \text{ eV}.$

b) Di getto posso scrivere che:

$\Phi_{bi} = \frac{q N_D}{2\epsilon_1} x_{np}^2 + \frac{q N_A}{2\epsilon_2} x_{pn}^2$ [l'elettrostatica è identica alla p-n, cambia solo ϵ].

$\hookrightarrow x_{pn} = x_{np} \frac{N_D}{N_A} \rightarrow \Phi_{bi} = \frac{q N_D}{2\epsilon_1} x_{np}^2 + \frac{q N_A}{2\epsilon_2} \frac{N_D^2}{N_A^2} x_{np}^2 =$

$= \frac{q N_D}{2} x_{np}^2 \left[\frac{1}{\epsilon_1} + \frac{N_D}{\epsilon_2 N_A} \right] = \Phi_{bi} \rightarrow x_{np} = \sqrt{\frac{2}{q N_D} \frac{\epsilon_1 \epsilon_2 N_A}{\epsilon_1 N_D + \epsilon_2 N_A} \Phi_{bi}}$

$= 48,8 \text{ nm}$;

$x_{pn} = x_{np} \frac{N_D}{N_A} = 183,2 \text{ nm}.$

c) L'obiettivo è: calcolare la w .

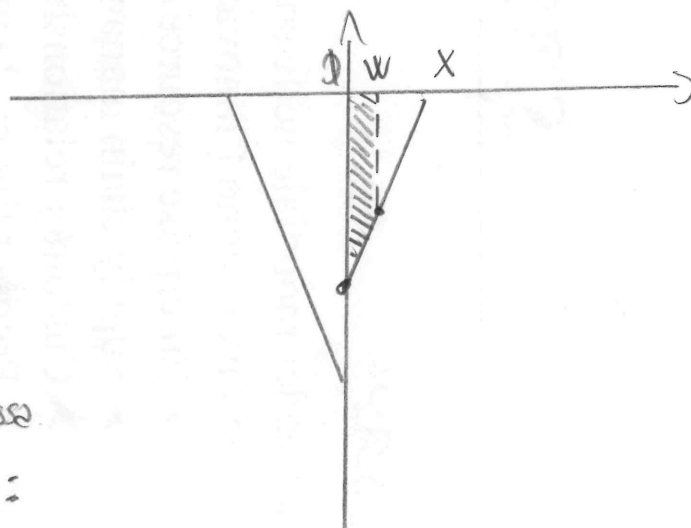
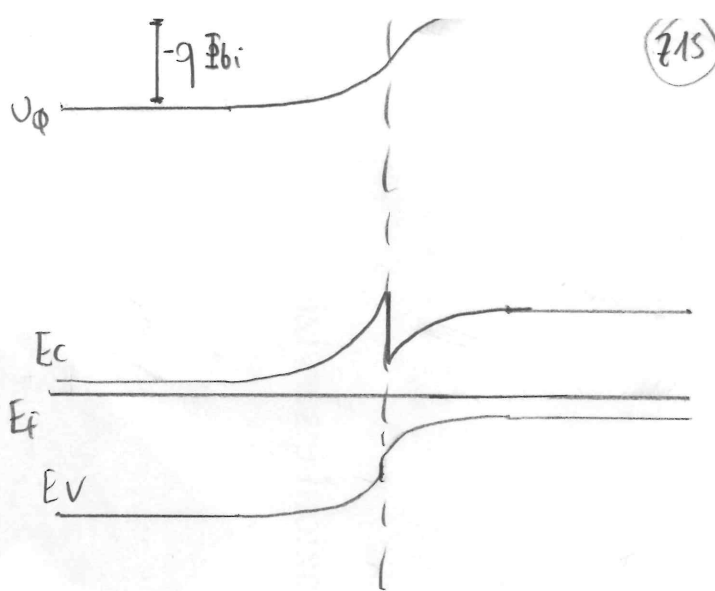
Un modo è partire dal campo $\mathcal{E}$ nel semiconduttore p:

$\mathcal{E}(x) = \int \frac{-q N_A}{\epsilon_2} dx = -\frac{q N_A}{\epsilon_2} [x - x_{pn}]$;

L'area tratteggiata è la $\Delta\Phi$ che ci interessa.

Come si può fare? Beh: area del trapezio =

$\Delta\Phi = \frac{1}{2} [\mathcal{E}(w) + \mathcal{E}(0)] \cdot w$ dove tutto è noto tranne w !



So che:

$$\phi(\phi) = \frac{qNA}{\epsilon_2} x_{pp}; \quad \phi(w) = -\frac{qNA}{\epsilon_2} [w - x_{pp}] = \frac{qNA}{\epsilon_2} [x_{pp} - w];$$

$$\hookrightarrow \Delta\phi = w \cdot \frac{1}{2} \left[2 \frac{qNA}{\epsilon_2} x_{pp} - \frac{qNA}{\epsilon_2} w \right] = \frac{qNA}{\epsilon_2} \left[2x_{pp} - w \right] \frac{w}{2}$$

$$\rightarrow \frac{w}{2} [2x_{pp} - w] = \frac{\epsilon_2}{qNA} \Delta\phi;$$

$$w^2 - 2x_{pp}w + \frac{2\epsilon_2}{qNA} \Delta\phi = \phi$$

$$\hookrightarrow w = x_{pp} - \sqrt{x_{pp}^2 - \frac{2\epsilon_2}{qNA} \Delta\phi}$$

d) Considera al posto di x_{pp} , le $x_p(V_d)$:

$$\hookrightarrow (w - x_p) = -\sqrt{\dots} \xrightarrow{0^2} w^2 - 2wx_p + x_p^2 = x_p^2 - \frac{2\epsilon_2}{qNA} \Delta\phi$$

$$\hookrightarrow x_p = \frac{w}{2} + \frac{\epsilon_2}{qNAw} \Delta\phi.$$

Ma:

$$x_p = \sqrt{\frac{2\epsilon N_{eq}}{qNA_2^2} (\phi_i - V_d)} \rightarrow \phi_i - V_d = x_p^2 \cdot \frac{qNA_2^2}{2\epsilon N_{eq}}$$

$$\hookrightarrow V_d = \phi_i - \frac{qNA_2^2}{2\epsilon N_{eq}} x_p^2 = \phi_i - \frac{qNA_2^2}{2\epsilon N_{eq}} \left[\frac{w}{2} + \frac{\epsilon_2}{qNAw} \Delta\phi \right]^2.$$

e) Ciò si può girare, con $V_d = \phi_i$ esplicitando N_{eq} e portando tutti gli NA_2 da una parte. Purtroppo però $\phi_i \propto \ln(NA_2)$, dunque l'espressione non è risolvibile se non con metodi numerici.

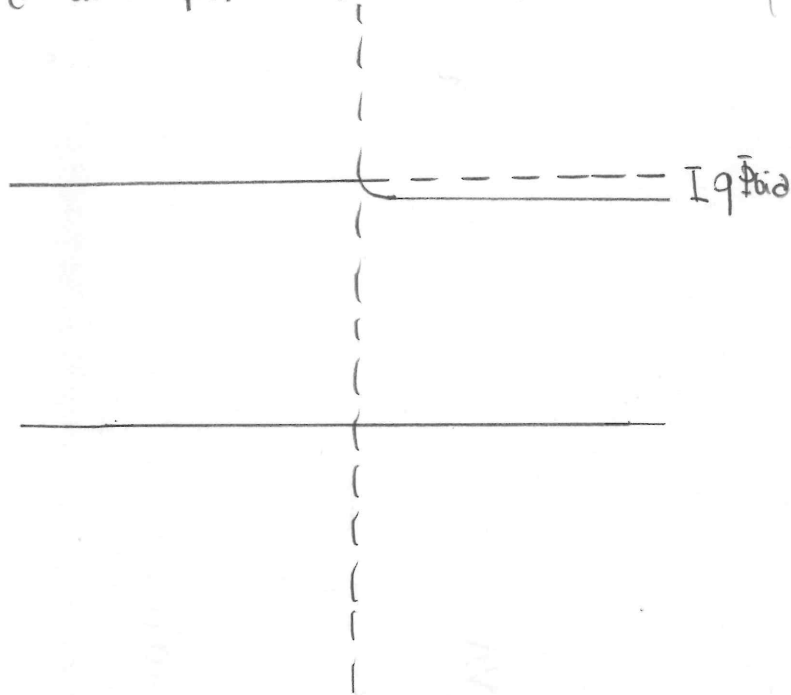
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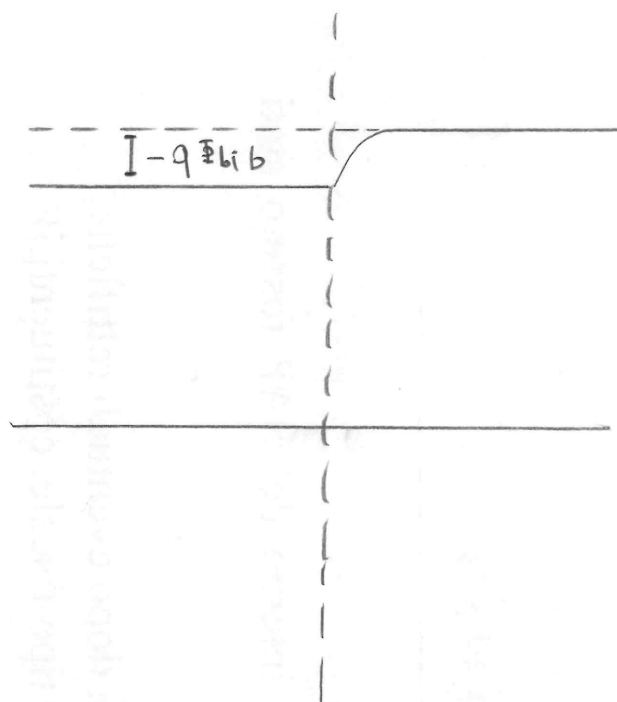
Esercizio 2

Da una parte ho Al ($q\Phi_M = 6.1 \text{ eV}$); dall'altra, altro.

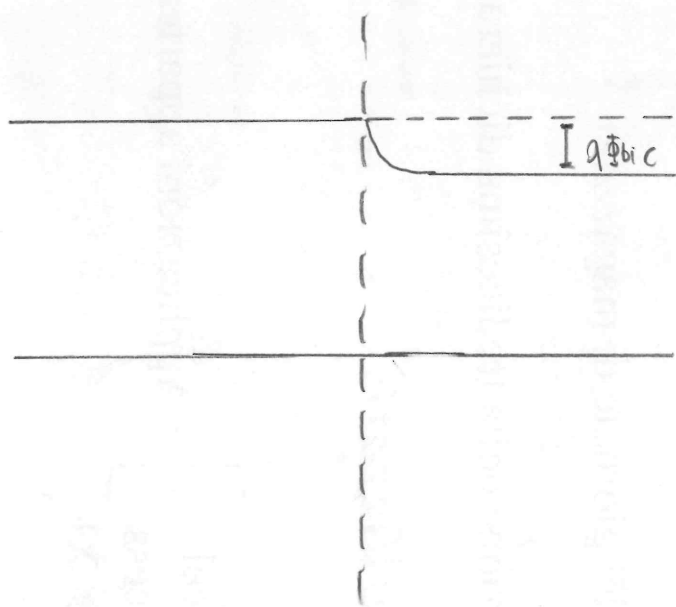
a



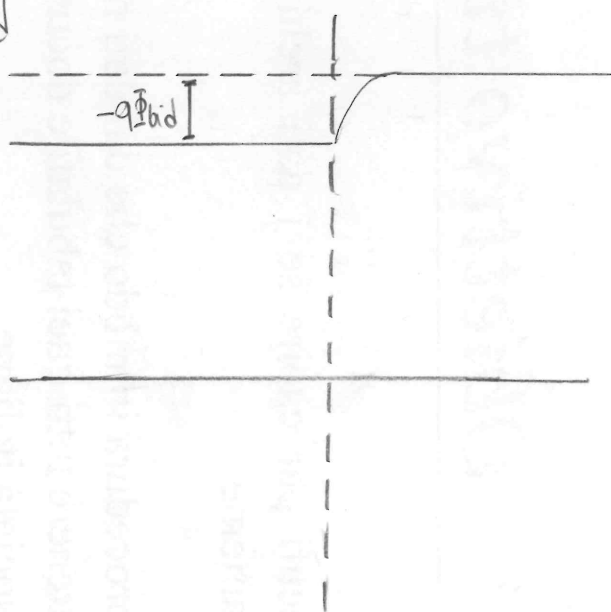
b



c



d



Nei casi "n":

$$q\Phi_{bi} = q\Phi_M - q\Phi_{sn} = q\Phi_M - [q\chi_s + (E_c - E_F)] = q\Phi_M - q\chi_s + k_B T \ln\left(\frac{N_D}{N_c}\right);$$

Nei casi "p":

$$q\Phi_{bi} = q\Phi_M - q\Phi_{sp} = q\Phi_M - [q\chi_s + E_g - (E_F - E_v)] = q\Phi_M - q\chi_s - E_g + k_B T \ln\left(\frac{N_A}{N_v}\right)$$

Calcolo dunque le quattro barriere:

$$q\Phi_{bi a} = 0,07517 \text{ eV}$$

$$q\Phi_{bi b} = -1,499 \text{ eV}$$

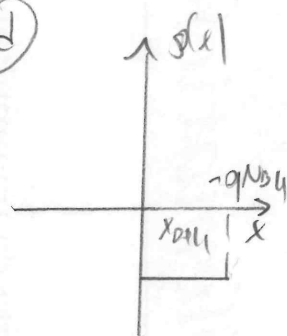
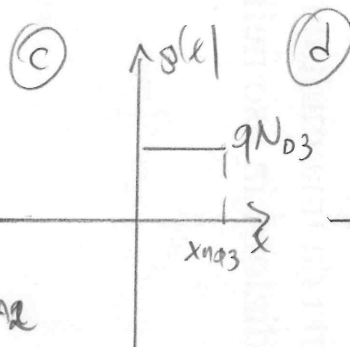
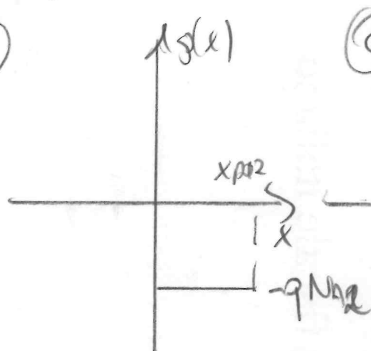
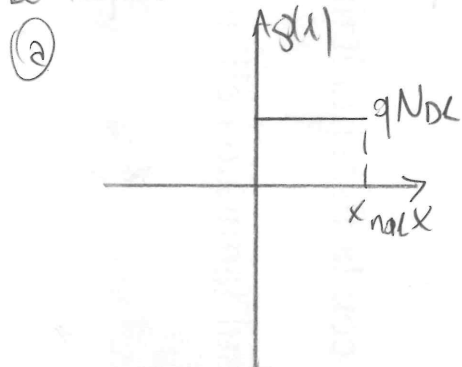
$$q\Phi_{bi c} = 0,382 \text{ eV}; q\Phi_{bi d} = -1,454 \text{ eV}$$

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I disegni sono fatti dopo questi calcoli.

Tutte e quattro le strutture presentano, come si evince dai diagrammi a bande, una regione di svuotamento nel semiconduttore. Ciò per la teoria di Schottky con l'aver raddrizzamento.

Le densità di carica saranno:



x_i si calcola da formulario:

$$x_d = \sqrt{\frac{2\epsilon}{qN_0} (V_{bi} - V)}$$

$\rightarrow$ $x_{d1} = 45,82 \text{ nm};$
 $x_{d2} = 204,6 \text{ nm};$

$$x_{d3} = 99,76 \text{ nm};$$

$$x_{d4} = 191,6 \text{ nm}.$$

Essendo tutte raddrizzanti,

$$J_1 = 57,77 \text{ kA/cm}^2 \text{ [enorme]}$$

$$J_2 = 281 \text{ mA/cm}^2$$

$$J_3 = 281,8 \text{ mA/cm}^2$$

$$J_4 = 1,654 \text{ fA/cm}^2$$

calcolo tutte le correnti:

$$\begin{cases} q\Phi_{B1,2} = 0,136 \rightarrow 1,396 & (a) \quad (b) \\ q\Phi_{B3,4} = 0,654 \rightarrow 1,306 & (c) \quad (d) \end{cases}$$

Nota: per (a) e (b) si ha un E_{B1} e per (c) e (d) un'altra, poiché esse dipendono solo dai materiali. Per b e d, dovrò usare la "barriera complementare a E_g ".

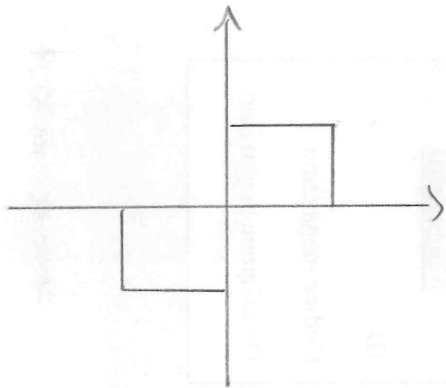
$$[q\Phi_B] = \text{eV}.$$

$$\begin{aligned} q\Phi_{bi} &= q\Phi_2 - q\Phi_1 = [q\chi_2 + (E_c - E_f)] - \\ &+ [q\chi_1 + E_{g1} - (E_f - E_v)] = \\ &= q\Delta\chi - E_{g1} + k_B T \ln \left(\frac{N_{D2} N_{v1}}{N_{D1} N_{A1}} \right) = \\ &= -1.231 \text{ eV}. \end{aligned}$$

$$\Delta E_c = -q\Delta\chi = -0.32 \text{ eV};$$

$$\Delta E_v = -\Delta E_g - q\Delta\chi = -50 \text{ meV}.$$

A questo punto, per le regioni svuotate,
derivo tutta la fantomina!



Nota: in questo ambito, ho $N_{A1} = N_{D2}$.

Ciò ci aiuta, poiché:

$$qN_{A1} x_{pp} = qN_{D2} x_{np} \rightarrow x_{pp} = x_{np}!$$

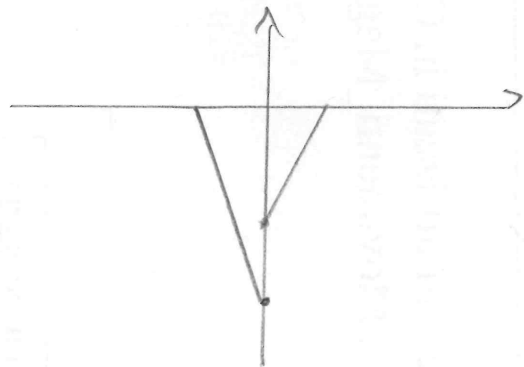
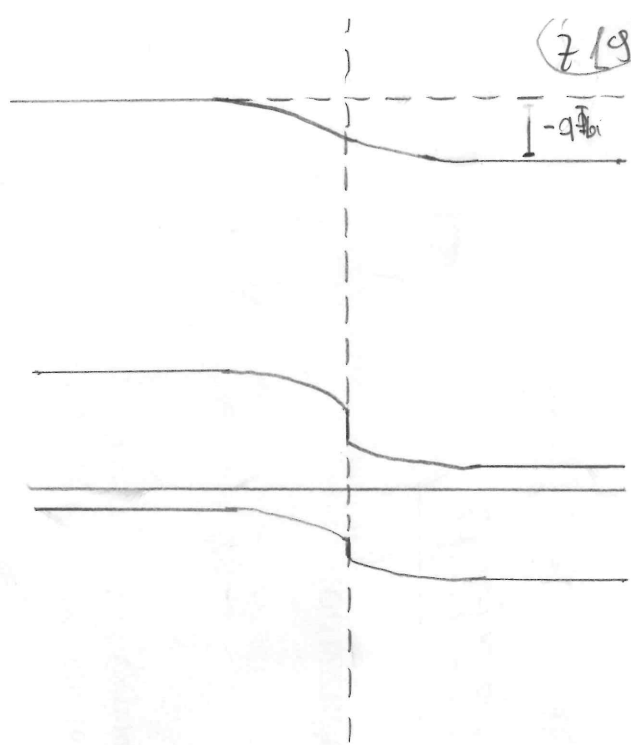
$$\hookrightarrow \Phi_{bi} = \frac{qN_{D2}}{2\epsilon_2} x_{np}^2 + \frac{qN_{A1}}{2\epsilon_1} x_{pp}^2 =$$

$$= \frac{qN_{D2}}{2} x_{np}^2 \left[\frac{1}{\epsilon_2} + \frac{1}{\epsilon_1} \right]$$

$$\hookrightarrow x_{np} = \sqrt{\frac{2}{qN_{D2}} \epsilon_1 \oplus \epsilon_2}.$$

b) $E_{11} \perp E_{12}$: il campo massimo
sarà nel "1" $\rightarrow$

$$\theta_{max} = \theta(\phi^-) = \frac{-qN_A}{\epsilon_1} x_{pp}$$



c) Ne ricavo una, e l'altra per dualità. So che:

(220)

$$n_p(x_p) p_n(x_n) = N_{c1} \exp\left(-\frac{E_c(x_p) - E_F}{k_B T}\right) N_{v2} \exp\left(-\frac{E_F - E_v(x_n)}{k_B T}\right) =$$

$$= N_{c1} N_{v2} \exp\left(\frac{E_v(x_n) - E_c(x_p)}{k_B T}\right);$$

So, dal d. e bande, che:

$$-[E_v(x_n) - E_c(x_p)] = q\Phi_{bi} + \Delta E_c + E_{g2} = q\Phi_{bi} + \Delta E_v + E_{g2}.$$

Considero $p_n(x_n)$:

$$n_n(x_n) p_n(x_n) \approx N_{D2} p_n(x_n) = N_{c2} N_{v2} \exp\left(-\frac{E_{g2}}{k_B T}\right)$$

$$\hookrightarrow p_n(x_n) \approx \frac{N_{c2} N_{v2}}{N_{D2}} \exp\left(-\frac{E_{g2}}{k_B T}\right);$$

$$\hookrightarrow n_p(x_p) p_n(x_n) \Rightarrow n_p(x_p) = \frac{N_{D2}}{N_{c2} N_{v2}} N_{c1} N_{v2} \exp\left(-\frac{E_{g2}}{k_B T}\right) \exp\left(-\frac{q\Phi_{bi} + \Delta E_v + E_{g2}}{k_B T}\right).$$

$$\Rightarrow n_p'(x_p) = \frac{N_{c1}}{N_{c2}} N_{D2} \exp\left(-\frac{q\Phi_{bi} + \Delta E_v}{k_B T}\right) \left[\exp\left(\frac{V_A}{V_T}\right) - 1\right].$$

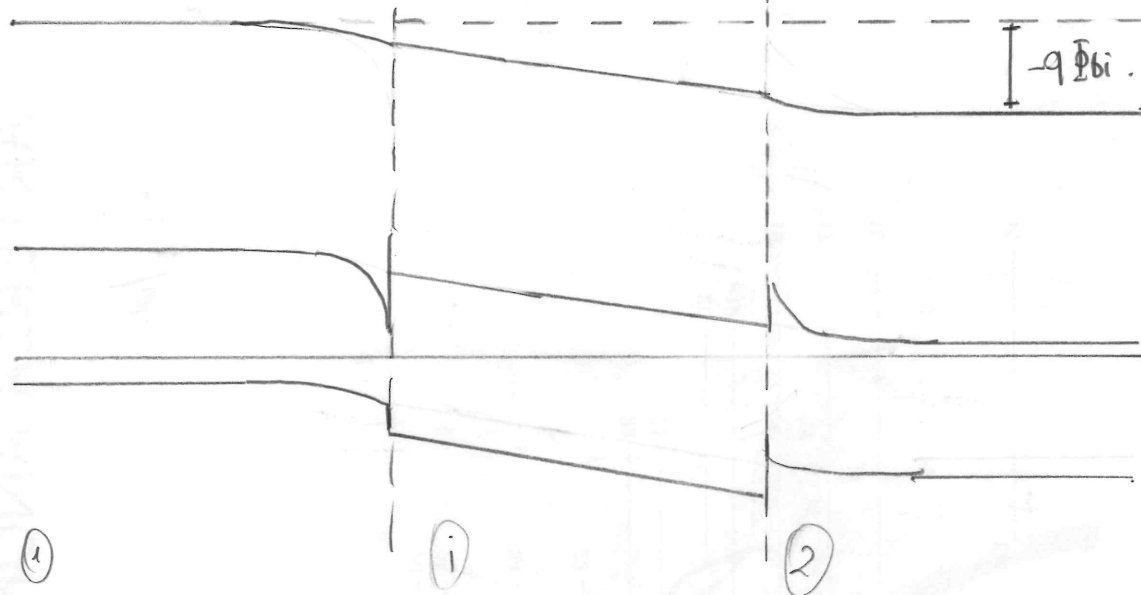
per dualità:

$$p_n'(x_n) = \frac{N_{v2}}{N_{v1}} N_{A1} \exp\left(-\frac{q\Phi_{bi} + \Delta E_v}{k_B T}\right) \left[\exp\left(\frac{V_A}{V_T}\right) - 1\right].$$

Dunque:

$$\frac{p_n'(x_n)}{n_p'(x_p)} = \frac{N_{v2} N_{c2} N_{A1}}{N_{v1} N_{c1} N_{D2}} \exp\left(-\frac{\Delta E_v - \Delta E_c}{k_B T}\right)$$

Esercizio
a)



$$q\Phi_{bi} = q\Phi_2 - q\Phi_1 = [q\chi_2 + |E_c - E_f|] - [q\chi_1 + E_{gc} - (E_f - E_v)] =$$

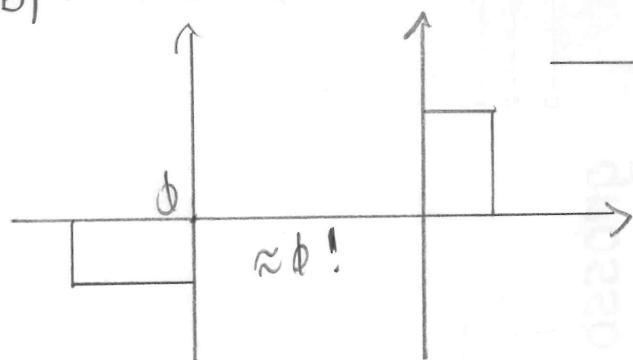
$$= -E_{gc} + k_B T \ln \left(\frac{N_c N_{vc}}{N_{ac} N_{dv}} \right) = -1.218 \text{ eV.}$$

$$\Delta E_g = 0.134 \text{ eV}$$

$$\Delta E_c = 0.204 \text{ eV}$$

$$\Delta E_v = 0.136 \text{ eV.}$$

b) Si consideri la seguente ϕ :



$\rightarrow \Phi_i:$

$$\int -\frac{qN_A}{\epsilon_L} dx = -\frac{qN_A}{\epsilon_L} [x - x_{p\phi}];$$

$$\int \frac{qN_D}{\epsilon_L} dx = \frac{qN_D}{\epsilon_L} [x - x_{n\phi}];$$

$$\phi(\phi) = \phi(\phi^+) \frac{\epsilon_2}{\epsilon_L} \rightarrow \phi(\phi^+) = \phi(\phi) \frac{\epsilon_L}{\epsilon_2} = \frac{qN_D}{\epsilon_L} x_{p\phi} \quad (x_{p\phi} < \phi!)$$

$$\rightarrow \phi(\phi^+) = \frac{qN_D}{\epsilon_L} x_{p\phi}.$$

$$\Phi_{bi} = \underbrace{\left(-\frac{qN_A}{\epsilon_L} x_{p\phi} \right)}_i + \underbrace{\left(\frac{qN_D}{2\epsilon_L} x_{p\phi}^2 \right)}_p - \underbrace{\left(\frac{qN_D}{2\epsilon_L} x_{n\phi}^2 \right)}_h$$

ma: $x_{n\phi} = -x_{p\phi} \frac{N_A}{N_D}$

$$\rightarrow \frac{qNA}{\epsilon_2} x_{pf} w_i + \frac{qNA}{2\epsilon_1} x_{pf}^2 + \frac{qNA^2}{2\epsilon_1 N_0} x_{pf}^2 = \Phi_{bi}$$

$$\rightarrow x_{pf}^2 \left[\frac{qNA}{2\epsilon_1} + \frac{qNA^2}{2\epsilon_1 N_0} \right] + \frac{qN_0}{\epsilon_2} w_i x_{pf} - \Phi_{bi} = 0$$

$$\rightarrow x_{pf}^2 \left[\frac{qN_0 N_0 + qNA^2}{2\epsilon_1 N_0} \right] + \frac{qNA}{\epsilon_2} w_i x_{pf} - \Phi_{bi} = 0$$

$$\rightarrow x_{pf}^2 + x_{pf}$$

Tema di esame 04/02/10 - Esercizio

a)

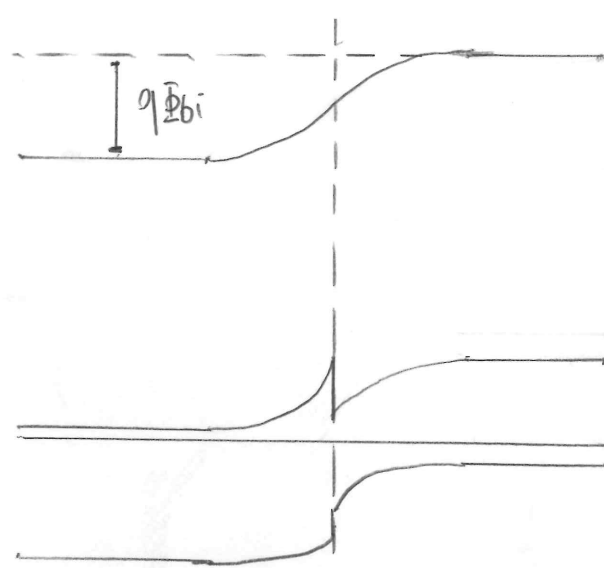
$$\Delta E_g = 0,34 \text{ eV}$$

$$\Delta E_c = 0,204 \text{ eV}$$

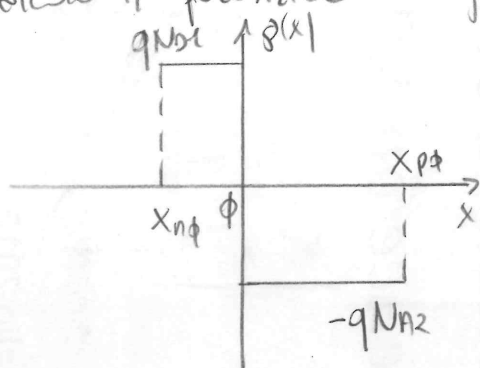
$$\Delta E_v = 0,136 \text{ eV}$$

$$q\Phi_{bi} = q\Phi_2 - q\Phi_1 = [q\chi_2 + E_{g2} - (E_f - E_v)] - [q\chi_1 + (E_c - E_f)] =$$

$$= q\Delta\chi + E_{g2} + k_B T \ln\left(\frac{N_{D1}N_{A2}}{N_{C1}N_{V2}}\right) = 1,68 \text{ eV}$$



b) Calcolo il potenziale in ogni zona. Sceglio come riferimento $\phi(+\infty)$.



per $x > x_{pf}$, $\phi(x) = \phi$;

per $0 < x < x_{pf}$, ho:

$$\phi(x) = \int \frac{-qNa_2}{\epsilon_2} dx = -\frac{qNa_2}{\epsilon_2} [x - x_{pf}]$$

$$\phi(x) = \frac{qNa_2}{2\epsilon_2} [x - x_{pf}]^2 \rightarrow \phi(\phi) = \frac{qNa_2}{2\epsilon_2} x_{pf}^2$$

Per $x < x_{np}$, ho:

$$\phi(x) = \int \frac{qNd_1}{\epsilon_1} dx = \frac{qNd_1}{\epsilon_1} [x - x_{np}] \rightarrow \phi(x) = -\frac{qNd_1}{2\epsilon_1} [x - x_{np}]^2 + C$$

c può esser stabilita imponendo la continuità del potenziale:

$$\phi(\phi^-) = \phi(\phi^+) \Rightarrow -\frac{qNd_1}{2\epsilon_1} x_{np}^2 + C = \frac{qNa_2}{2\epsilon_2} x_{pf}^2$$

$$\hookrightarrow \phi(x) = -\frac{qNd_1}{2\epsilon_1} [x - x_{np}]^2 + \frac{qNa_2}{2\epsilon_2} x_{pf}^2 + \frac{qNd_1}{2\epsilon_1} x_{np}^2$$

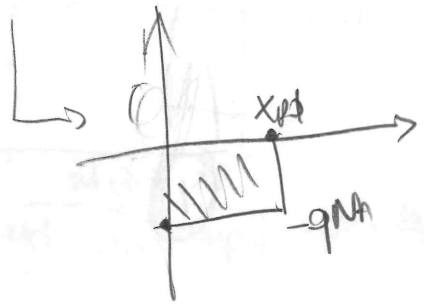
$$\text{Per } x < x_{np}, \phi(x) = \Phi_{bi} = \frac{qNa_2}{2\epsilon_2} x_{pf}^2 + \frac{qNd_1}{2\epsilon_1} x_{np}^2$$

Uso questa e la neutralità globale: $x_{pf} = x_{np} \frac{Nd_1}{Na_2}$

$$\hookrightarrow \Phi_{bi} = \frac{qNa_2}{2\epsilon_2} \frac{Nd_1^2}{Na_2^2} x_{np}^2 + \frac{qNd_1}{2\epsilon_1} x_{np}^2 \rightarrow x_{np}^2 \frac{qNd_1}{2} \left[\frac{Nd_1}{\epsilon_2 Na_2} + \frac{1}{\epsilon_1} \right]$$

$$\rightarrow x_{np} = \sqrt{\frac{2}{qNd_1} \frac{\epsilon_1 \epsilon_2 Na_2}{\epsilon_1 Nd_1 + \epsilon_2 Na_2}} = \sqrt{\frac{2}{qNd_1^2} \frac{\epsilon_1 \epsilon_2 Nd_1 Na_2}{\epsilon_1 Nd_1 + \epsilon_2 Na_2}}$$

Provo a calcolare il potenziale per bene;



$$\phi(x) = \int \frac{-qNA}{\epsilon_2} dx = -\frac{qNA}{\epsilon_2} [x - x_{pp}] ;$$

$$\phi(x) = -\int \frac{q}{\epsilon_2} dx = -\frac{qNA}{2\epsilon_2} [x - x_{pp}]^2$$

$$-q\phi(x) = -\frac{q^2 NA}{2\epsilon_2} [x - x_{pp}]^2$$

$$E_c(\phi^-) - E_c(\phi^+) = \phi_{BE} - \Delta E_c = q\Delta x$$

$$E_c(\phi^+) = E_c(\phi^-) - \Delta E_c; \quad E_c(\phi^+) = -q\phi(\phi^-)$$

$$\rightarrow \phi(\phi^-) = \frac{qNA}{2\epsilon_2} x_{np}^2 ;$$

$$\rightarrow E_c(\phi^+) = -\frac{q^2 NA}{2\epsilon_2} x_{np}^2 - \Delta E_c$$

$$E_c(\phi^-) - E_c(\phi^+) = q\Delta E_c ;$$

$$E_c(+\infty) \text{ ref ;}$$

$$q\phi(x) = E_c(w) - E_c(+\infty) = (E_c(\phi^+) - E_c(+\infty))$$

$$q\Delta E_c = E_c(\phi^-) - E_c(\phi^+) = E_c(\phi^-) + E_c(+\infty) - E_c(+\infty) - E_c(\phi^+)$$

$$\rightarrow q\Delta E_c = q\Delta E = q\phi(\phi^-) - q\phi(\phi^+) = q\phi(\phi^-) - q\phi(w)$$

$$\rightarrow \phi(w) - \phi(\phi^-) + \Delta E = \phi$$

MA:

$$\phi(x) = \frac{qNA}{2\epsilon} x^2 - \frac{qNAx_d}{\epsilon} x + K$$

$$\rightarrow \frac{qNA}{2\epsilon} w^2 - \frac{qNAx_d}{\epsilon} w + \Delta E = \phi \rightarrow w = x_d - \sqrt{x_d^2 - \frac{2\epsilon}{qNA} \Delta E}$$

Trucco: ricondurre al problema

NOTA: conoscere $\phi(w)$

$$e \text{ da } d\phi = -q\phi$$

C. Discorsetto > ②

$$L \rightarrow N(E) = \gamma_P \sqrt{E_V - E} ; \quad f(E) = \left[1 + \exp\left(\frac{E - E_F}{k_B T}\right) \right]^{-1}$$

$$f_c(E) = 1 - f(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{k_B T}\right)}$$

$$\rightarrow P = \int_{-\infty}^{E_V} \frac{\gamma_P \sqrt{E_V - E}}{1 + \exp\left(\frac{E_F - E}{k_B T}\right)} dE \approx \int \gamma_P \exp\left(\frac{E - E_F}{k_B T}\right) \sqrt{E_V - E} dE$$

$$= \gamma_P \exp\left(\frac{-E_F}{k_B T}\right) \int \sqrt{E_V - E} \exp\left(\frac{E}{k_B T}\right) dE$$

Questo si scopre essere:

$$L_s = N \exp\left(\frac{E_V - E_F}{k_B T}\right)$$

$$n_i = N_c \exp\left(-\frac{E_C - E_F i}{k_B T}\right) \rightarrow n \propto n_i \exp\left(\frac{E_F - E_F i}{k_B T}\right)$$

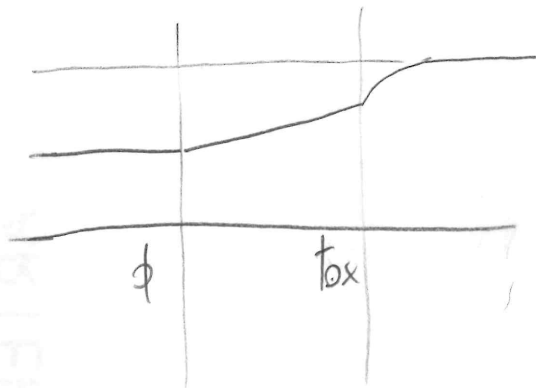
$$N_D = N_c \exp\left(-\frac{E_C - E_F}{k_B T}\right) ; \quad \frac{n_i^2}{N_D} = N_v \exp\left(-\frac{E_F - E_V}{k_B T}\right)$$

$$L \rightarrow n_p = n_i \exp\left(\frac{E_F - E_F i}{k_B T}\right) \quad \begin{aligned} n &= N_D \\ p &= \frac{n_i^2}{N_D} \end{aligned}$$

$$L \rightarrow \frac{N_D}{\frac{n_i^2}{N_D}} = \frac{N_p^2}{n_i^2} = \frac{N_c}{N_v} \exp\left(\frac{E_F - E_C + E_F - E_V}{k_B T}\right)$$

$$L \rightarrow N_D \propto n_i \exp\left(\frac{E_F - E_F i}{k_B T}\right) ; \quad E_F - E_F i = k_B T \ln\left(\frac{N_D}{n_i}\right)$$

$$E_F = E_F i + \dots$$



$$E(-\infty) = -qV_G;$$

$$E(+\infty) = -qV_B;$$

$$E(\text{tox}) = -q\phi_{ch} - q\phi_s;$$

$$E(-\infty) - E(\text{tox}) = -qV_G - (-q\phi_{ch} - q\phi_s) \Rightarrow V_G - 2\phi_p - \phi_{ch} = V_{ox};$$

$$E(\text{tox}) - E(+\infty) = -q\phi_{ch} - q\phi_s - (-qV_B) \Rightarrow \phi_{ch} + 2\phi_p - V_B.$$

$$\rightarrow Q_t = -Q_n - Q_d \Rightarrow Q_n = -Q_t - Q_d =$$

$$= -C_{ox}V_{ox} + \underbrace{qN_A x_p}_{\text{quantum } (p-n)!} = -C_{ox}(V_G - 2\phi_p - \phi_{ch}) + \sqrt{2qN_A \epsilon_s (\phi_{ch} + 2\phi_p - V_B)}$$

$$\rightarrow \phi_{ch} = \phi; \quad Q_n = \phi \Rightarrow V_G = 2\phi_p + \sqrt{2qN_A \epsilon_s (2\phi_p - V_B)}$$

$$= V_{Thp} + \frac{\sqrt{2qN_A \epsilon_s (2\phi_p - V_B)} - \sqrt{2qN_A \epsilon_s (2\phi_p)}}{C_{ox}}$$

$$I_D = W \oint J_n(x, y) = \text{drift} = W \int q \mu_n n \frac{\partial \phi(y)}{\partial y} dx = q \mu_n W N(y) \frac{\partial \phi}{\partial y};$$

$$I_D = \frac{q \mu_n W}{L} \int N(y) d\phi_{ch} = \frac{\mu_n C_{ox} W}{L} \int (V_{GS} - \phi_{ch} - V_{Th}) d\phi_{ch} =$$

$$= \frac{\mu_n C_{ox} W}{L} \left[(V_{GS} - V_{Th}) V_{DS} - \frac{V_{DS}^2}{2} \right].$$

Alcune note per provar a copir meglio l'eterostruttura;

$$\Delta E_g \triangleq E_{g2} - E_{g1};$$

$$\Delta \chi = \chi_2 - \chi_1.$$

$$\begin{aligned} \rightarrow \Delta E_c &= E_{c2} - E_{c1} = \{[V_0 - E_{c2}] - [V_0 - E_{c1}]\} = \{-q\chi_2 - (-q\chi_1)\} = \\ &= -q[\chi_2 - \chi_1] = \boxed{-q\Delta\chi} \end{aligned}$$

$$\Delta E_v = -q\Delta\chi - \Delta E_g.$$

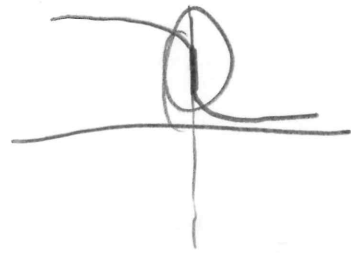
Se $\chi_2 - \chi_1 > \phi$, allora

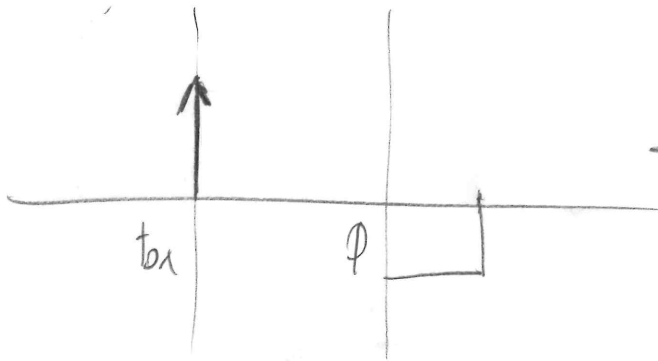
$$\boxed{\Delta E_c = E_{c2} - E_{c1} \quad L\phi!}$$

questo vuol dire che:

@ junction. $E_{c2} > E_{c1}$

OK???





$$\phi(x) = \int -\frac{qNA}{\epsilon_s} dx =$$

$$= -\frac{qNA}{\epsilon_s} [x - x_d] ;$$

$$\rightarrow \phi(x) = \frac{qNA}{2\epsilon_s} [x - x_d]^2 ;$$

$$\phi(\phi^{-1}) = \frac{qNA}{\epsilon_s} x_d ; \quad \phi(\phi^{-1}) = \frac{qNA}{\epsilon_{ox}} x_d ;$$

$$\phi(x) \Big|_{ox} = -\frac{qNA}{\epsilon_{ox}} x_d x ;$$

$$\rightarrow \Phi_{bi} = \frac{qNA}{2\epsilon_s} x_d^2 + \frac{qNA}{\epsilon_{ox}} x_d t_{ox}$$

$$\rightarrow x_d^2 + \frac{2\epsilon_s}{\epsilon_{ox}} x_d t_{ox} - \frac{2\epsilon_s}{qNA} \Phi_{bi} =$$

$$\rightarrow x_d = -\frac{\epsilon_s}{\epsilon_{ox}} t_{ox} \pm \sqrt{\left(\frac{\epsilon_s}{\epsilon_{ox}} t_{ox}\right)^2 + \frac{2\epsilon_s}{qNA} \Phi_{bi}}$$

$$\frac{d^2 \phi}{dx^2} = \frac{g(x)}{\epsilon_s} ; \quad g(x) = q(p - n - N_A^-) ; \quad n_{np} = n_i \exp\left(\frac{-\phi_p}{k_B T}\right) ;$$

$$p_{np} = n_i \exp\left(\frac{\phi_p}{k_B T}\right) ;$$

$$N_A^- = p_{np} - n_{np} ;$$

$$p = n_i \exp\left(-\frac{E_F - E_{Fi}}{k_B T}\right) ; \quad n = n_i \exp\left(\frac{E_F - E_{Fi}}{k_B T}\right) ;$$

$$p(x) = n_{np} \exp\left(\frac{q\phi(x) - q\phi_p}{k_B T}\right) ;$$

$$\rightarrow p(x) = n_{np} \exp\left(-\frac{U(x)}{V_T}\right) ;$$

$$\text{define } E_{Fi}(x) - E_F \triangleq -q\phi(x)$$

$$\rightarrow p = n_i \exp\left(\frac{q\phi(x)}{k_B T}\right) ; \quad n = n_i \exp\left(-\frac{q\phi(x)}{k_B T}\right) ;$$

16/02/24

$$\rightarrow g = \frac{1}{n \mu_n q} + \frac{1}{p \mu_p q}$$

n e p dipende da T ;

μ_n e μ_p dipendono dal drogaggio;
cio' dipende da N ;

17/02/24

$$\Delta r \equiv \Delta r_f ; \Delta r_f = \gamma_F b ;$$

$$I_E = I_{n \text{ diff}} + I_{p \text{ diff}} ; \gamma_F = \frac{I_n}{I_n + I_p} \rightarrow I_E = \frac{I_n}{\gamma_F}$$

$$\rightarrow I_E = \frac{I_{n \text{ diff}}}{\gamma_F} ; I_C = I_{n \text{ diff}} + I_{p \text{ diff}} = b I_{n \text{ diff}} = I_E \gamma_F b$$

$$I_D = I_{D0} \left[\exp\left(\frac{V_A}{V_T}\right) - 1 \right]$$

$$\rightarrow \frac{\partial I_D}{\partial V_A} = \frac{I_{D0}}{V_T} \exp\left(\frac{V_A}{V_T}\right) = \frac{I_D + I_{D0}}{V_T}$$

$$V_G = 5V ; V_S = 2V ; V_D = 4.5V ;$$

$$V_{GS} = 3V ; V_{DS} = 1V \rightarrow V_{GS} - V_{TH} = 2V ; V_{DS} = 2.5V$$

quadr.

$$W = x_n(V_0) + \sqrt{\left[x_p(V_0)\right]^2 - \frac{2\varepsilon_2}{qNA} \Delta\Phi}$$

$$\rightarrow (W - x_p(V_0))^2 = x_p(V_0)^2 - \frac{2\varepsilon_2}{qNA} \Delta\Phi$$

$$\hookrightarrow W^2 - 2x_p(V_0)W = -\frac{2\varepsilon_2}{qNA} \Delta\Phi$$

$$\hookrightarrow x_p(V_0') = \frac{W}{2} + \frac{\varepsilon_2}{qNAW} \Delta\Phi$$

~~$$\frac{2(\Phi_i - V_0)}{qNA^2} \varepsilon_{Neg}$$~~

$$= |\Phi_i - V_0| = \left[\frac{W}{2} + \frac{\varepsilon_2}{qNAW} \Delta\Phi \right]^2 \frac{2\varepsilon_{Neg}}{qNA^2}$$

~~$$\hookrightarrow |\Phi_i - V_0| = \left[\frac{W}{2} + \frac{\varepsilon_2}{qNAW} \Delta\Phi \right]^2 \frac{2\varepsilon_{Neg}}{qNA^2}$$~~

(Eine) Alpensymphonie

Alpine Symphony

Sinfonia delle Alpi

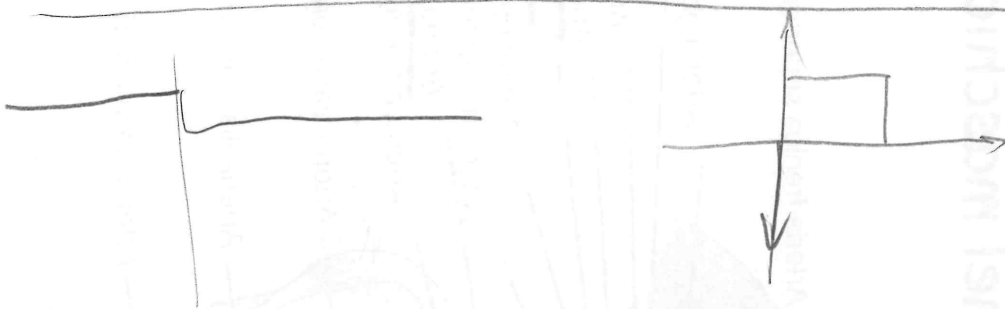
KEINE SYMPHONIE

$$q(p - n + N_D - N_A) = \phi;$$

$$\hookrightarrow n = \frac{p}{\beta} \rightarrow p^2 - (N_A - N_D)p - n_i^2 = \phi$$

$$\hookrightarrow \Delta = (N_A - N_D)^2 + 4n_i^2; \quad p = \frac{N_A - N_D}{2} \pm \sqrt{\frac{(N_A - N_D)^2 + 4n_i^2}{2}}$$

$$\sigma \quad p = \frac{N_A - N_D}{2} \pm \sqrt{\left| \frac{N_A - N_D}{2} \right|^2 + n_i^2} = \frac{N_A - N_D}{2} \left[1 \pm \sqrt{1 + \frac{4n_i^2}{(N_A - N_D)^2}} \right]$$



$$\hookrightarrow \Phi_{bi} = \frac{qN_D}{2\epsilon_s} x_d^2;$$

$$E_c(x) = q\Phi_B - \frac{q^2 N_D}{\epsilon_s} \left[x_d x - \frac{x^2}{2} \right]$$

$$J_{th} = A\phi T^2 \exp\left(-\frac{q\Phi_B}{k_B T}\right); \quad I_{SM} \propto n(\phi);$$

$$\hookrightarrow n(\phi) = N_C \exp\left(-\frac{q\Phi_B}{k_B T}\right); \quad n(\infty) = N_C \exp\left(\frac{E_F - E_C}{k_B T}\right)$$

$$\hookrightarrow n(\phi) = n(\infty) \exp\left(-\frac{q\Phi_B + E_C - E_F}{k_B T}\right)$$

$$= \frac{n(\infty)}{N_D} \exp\left(-\frac{qV_{bi}}{k_B T}\right)$$

